

## Electromagnetic Induction:-

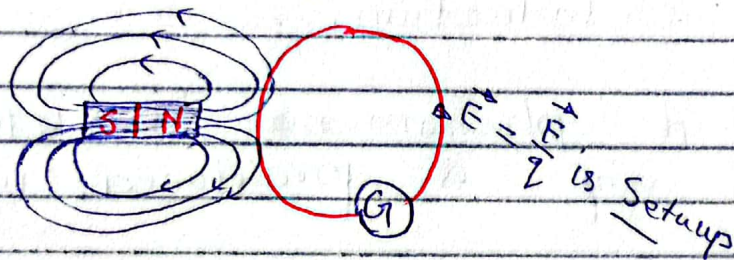
In 1831, Micheal Faraday  
prove experisimantly that  
whenever there is

$$\Phi = \vec{B} \cdot \vec{A}$$

$$\Phi = BA \cos \theta$$

$$\left(\frac{\Delta \Phi}{\Delta t}\right) = \mathcal{E}$$

change in magnetic flux, there  
is induced emf in the coil.



\* Faraday Law lighted the whole world.

Change in magnetic flux is responsible  
for induced emf.

For induce emf:-

(i) Change in magnetic flux  
is necessary

(ii) Flux linkage with coil is  
also necessary.

\* P



## Electromagnetic Induction:

[Current is induced due to relative motion of coil and magnet.]

"A phenomena in which induced emf is produced due to

relative motion of magnet and coil is called <sup>Electro</sup>magnetic Induction.

Def: A phenomena in which induced emf is produced in a

coil due to change in magnetic flux linking with the coil

is called Electromagnetic Induction.

Exam Ques

## Faraday's Law of

## Electromagnetic Induction:

- ① This Law states that "The magnitude of induced emf produced in a coil is directly proportional to the time



rate of change of magnetic flux, linking with the coil.

OR,

(2) This Law States that "the magnitude of induced emf produced in a coil is equal to the negative time rate of change of magnetic flux, linking with the coil."

Mathematically:-

$$E \propto \frac{\Delta \phi_m}{\Delta t}$$

$$E = \frac{K \phi_m}{\Delta t}$$

$$K = 1$$

$$E = \left( \frac{\phi_m}{\Delta t} \right)$$

$$E = - \left( \frac{\phi_m}{\Delta t} \right) \quad \text{---} \quad \textcircled{I}$$

The negative sign comes from Lenz law.

$$E = -N \left( \frac{\phi_m}{\Delta t} \right)$$

N = number of turn ...



$$\text{Flux linkage} = N \Phi_m$$

Lenz's

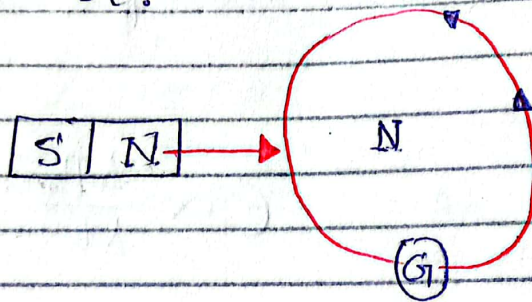
Law:-

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This Law States that

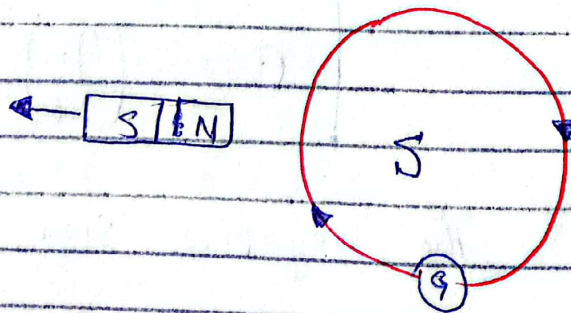
"The induced current in a coil is always produced in such a way that it will

oppose, by its magnetic field, the change in magnetic flux producing it.

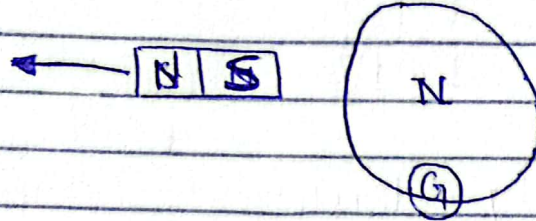
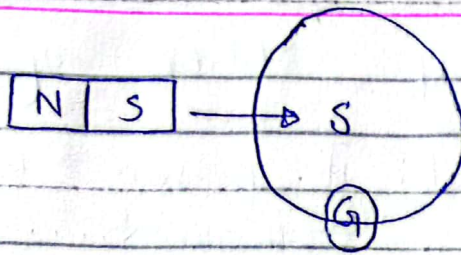


\* From direction of magnetic field we can determine direction of current.

\* The current in above case will be in Anti-clockwise direction.







\* Lenz's Law Satisfy / obey Law of Conservation of energy.

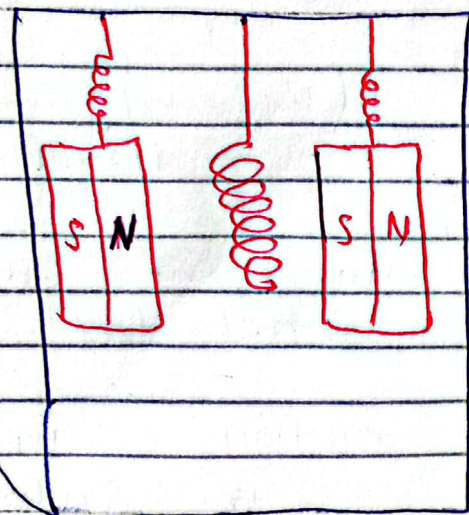
\* Lenz's law is natural Law.

\* We can also determine the direction of induced current by Right hand Fleming rules.

### Sesmometre :-

A device by which we can detect / measure the

Intensity of earthquake.



\* From the magnitude of induced emf, due to change in magnetic flux the Intensity of Earthquake can be determined.

Electromagnetic sesmometre





**Seismology:** Study of Earthquakes.

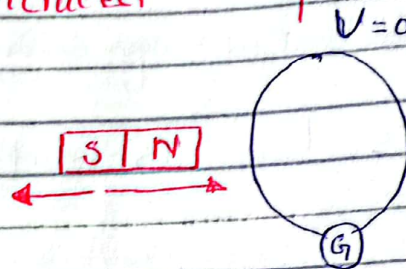
**Seismologist:** A person who study earthquakes....

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1. Statically Induced emf:

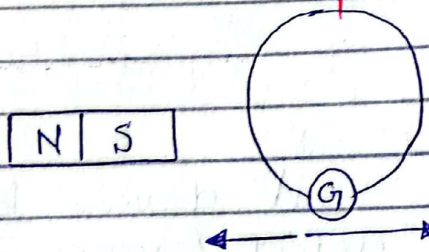
2. Dynamically Induced emf:

- ① Coil at Rest
- ② Magnet is moved



Statically Induced emf:

- ① Magnet at rest
- ② Coil is moved



Dynamically Induced emf

**Exam Ques**

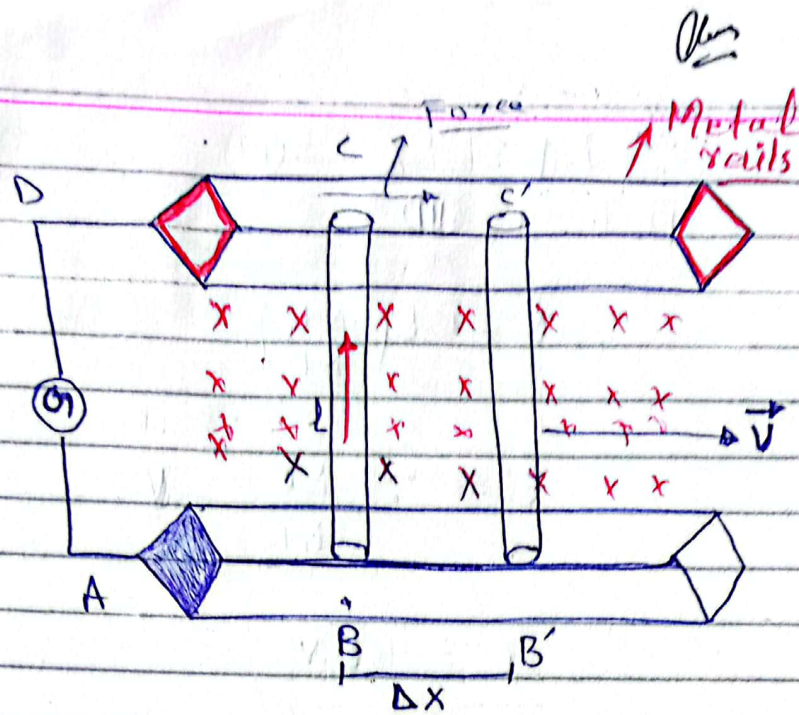
**Motional emf:** "Dynamically (Induced emf is called motional emf.)"

OR,

An emf induced in a conductor due to its

motion in a magnetic field is called Motional emf.





\* Emf is induced in the loop due to changing area...

$$\mathcal{E} = - \frac{N(\Delta\Phi)_m}{\Delta t} \quad \text{Lenz-or Faraday law.}$$

$$N = 1 \quad (\text{loop is one})$$

$$\mathcal{E} = - \left( \frac{\Delta\Phi_m}{\Delta t} \right) \quad \text{--- (1)}$$

$$\therefore \Phi_m = \vec{B} \cdot \vec{A}$$

$$\Phi_m = BA \cos\theta$$

$$\theta = 180^\circ \quad (\text{B/w } B \text{ and vector Area}).$$

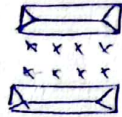
$$\Phi_m = -BA \quad \text{--- (2)}$$

put (2) in (1)

$$\mathcal{E} = - \frac{\Delta}{\Delta t} (-BA)$$

$$\mathcal{E} = B \left( \frac{\Delta A}{\Delta t} \right) \quad \text{--- (11) Because } \Phi \text{ changes due to } A.$$





$$\therefore \Delta A = L \Delta x \quad \text{--- (iv)}$$

put in (iii) :

$$\mathcal{E} = BL \left( \frac{\Delta x}{\Delta t} \right)$$

$$\leftarrow \text{v} \quad \therefore \frac{\Delta x}{\Delta t} = v$$

$$\mathcal{E} = BLv$$

$$\boxed{\mathcal{E}_m = vBL}$$

$\mathcal{E}_m = \text{motional emf.}$

$v = \text{velocity of conductor in magnetic field.}$

$B = \text{magnetic field (constant)}$

$L = \text{length of conductor (constant).}$

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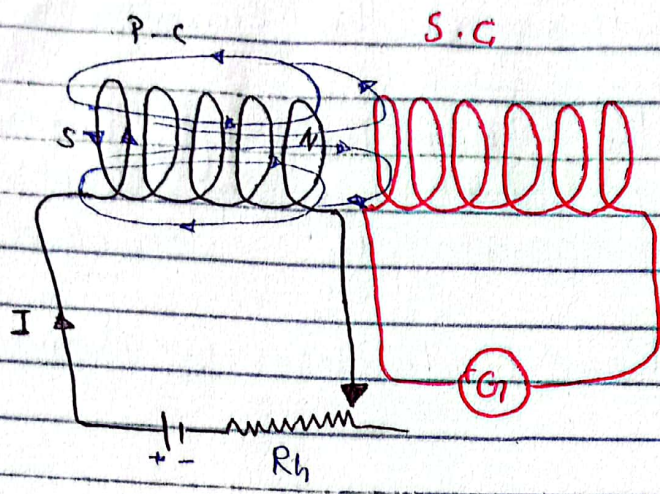
Mutual Induction:-

A phenomena in which an induced emf is produced in a secondary

coil by changing the current

(magnetic ~~flux~~ flux) in the primary coil is called induced emf. Mutual induction.





$$B = \mu_0 I$$

$$I = \frac{V}{R}$$

$$\Phi_m = \vec{B} \cdot \vec{A}$$

$$E = -N \left( \frac{\Phi_m}{\Delta t} \right)$$

$$E_s \propto \frac{\Delta I_p}{\Delta t}$$

$$E_s = -M \left( \frac{\Delta I_p}{\Delta t} \right) \quad \text{--- (1)}$$

M is constant, which is called coefficient of Mutual Induction.

$$M = - \frac{E_s}{\left( \frac{\Delta I_p}{\Delta t} \right)}$$

M (coefficient) is the ratio of induced emf in secondary coil to the rate of change of current in primary coil.

$$M = H \text{ (Henry)}$$

$$1H = \frac{1V}{\left( \frac{1A}{1s} \right)}$$

\* Negative sign shows the Lenz's law.



\* If we increase the current in primary coil, the direction of current in primary and secondary coil will be opposite to each other.

\* When current decreases in primary coil

As we have:

$$E_s = -N_s \left( \frac{\Delta \Phi_m}{\Delta t} \right) \quad \text{--- (iii)}$$

$$E_s = -\frac{\Delta}{\Delta t} (N_s \Phi_m) \quad \text{--- (ii)}$$

$$\text{(i)} \Rightarrow E_s = -\frac{\Delta}{\Delta t} (M I_p) \quad \text{--- (iv)}$$

Compare (iii) and (iv):

$$-\frac{\Delta}{\Delta t} (M I_p) = -\frac{\Delta}{\Delta t} (N_s \Phi_m)$$

$$M = \frac{N_s \Phi_m}{I_p}$$



coefficient of mutual induction

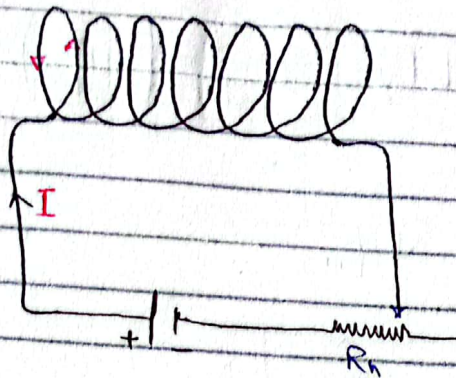
Another equation for coefficient of mutual induction

SELF INDUCTION:- A phenomena in

which an induced emf is produced in a coil by changing the current (magnetic flux) in the same coil is called self



## Induction.



$$E \propto \left( \frac{\Delta I}{\Delta t} \right)$$

$$E = -L \left( \frac{\Delta I}{\Delta t} \right) \quad \text{--- (1)}$$

$$E = -\frac{\Delta}{\Delta t} (LI) \quad \text{--- (1)}$$

$L$  = coefficient of ~~the~~ Self Induction

$$L = -\frac{E}{\left( \frac{\Delta I}{\Delta t} \right)}$$

$$1H = \frac{1V}{\left( \frac{1A}{1s} \right)}$$

From Faraday law:

$$E = -N \left( \frac{\Delta \phi_m}{\Delta t} \right)$$

$$E = -\frac{\Delta}{\Delta t} (N \phi_m) \quad \text{--- (2)}$$

$$\text{(1)} \Rightarrow E = -\frac{\Delta}{\Delta t} (LI) \quad \text{--- (3)}$$



Compare ② and ③

$$-\frac{N}{\Delta t} (LI) = -\frac{N}{\Delta t} (N\Phi_m)$$

$$LI = N\Phi_m$$

$$L = \frac{N\Phi_m}{I}$$

Coefficient of Mutual Induction  
(M):

Depends upon:

1. No of turns ( $N_s$ ).
2. Area of Secondary coil (A)
3. closeness of the two coil.

4. Nature of the coil (Material)  
"of the coil"

Exam Ques

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A.C Generator :-

1. Def: A device which convert mechanical energy into electrical energy is called A.C Generator.  
\* It is a source of emf.

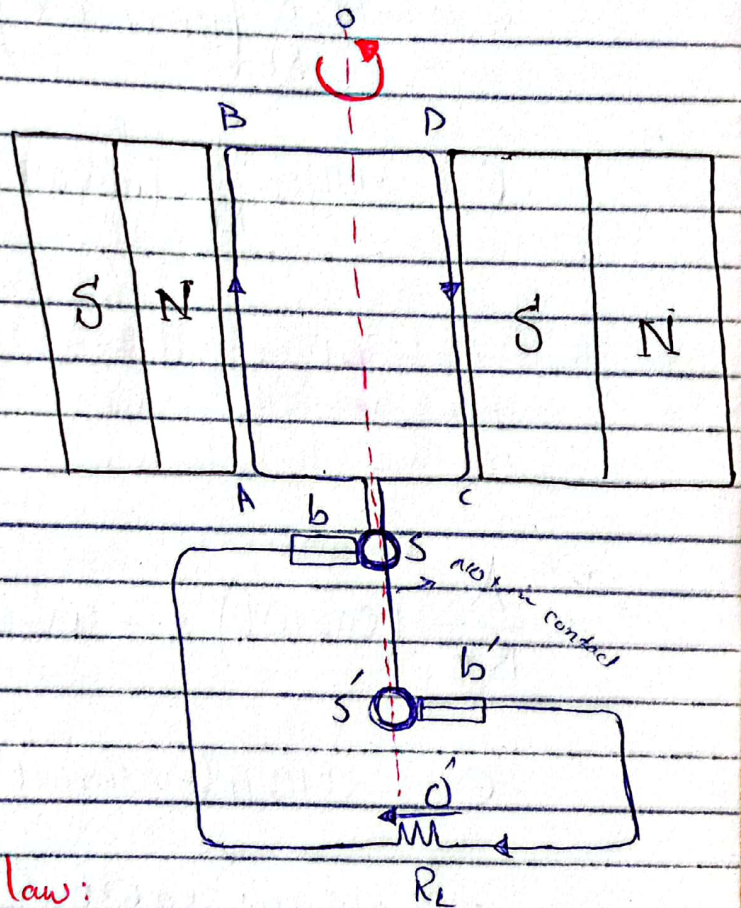
2. principle :-

It works on Faraday's Law of electromagnetic induction.



3. Construction: (i) permanent magnetic field  
 (ii) Rectangular coil (iii) Slip rings (iv) Two carbon brushes (v) load Resistance. (Pau. Regenerator)
4. Theory of working

### 5. Graphical Representation:



Applying Faraday's law:

$$\epsilon = -N \left( \frac{\Delta \Phi_m}{\Delta t} \right) \quad \text{--- (i)}$$

$$\Phi_m = \vec{B} \cdot \vec{A}$$

$$\Phi_m = BA \cos \theta \quad \text{--- (ii)}$$

In AC-generator we change  $\theta$ .



$$\text{As } \omega = \frac{\phi}{t}$$

$$\phi = \omega t \quad \text{--- (iii)}$$

$$\phi_m = BA \cos \omega t \quad \text{--- (iv)}$$

Put in (i):

$$\epsilon = -N \frac{\Delta}{\Delta t} (BA \cos \omega t)$$

$$\epsilon = -NBA \frac{\Delta}{\Delta t} (\cos \omega t) \quad \text{--- (v)}$$

We Replace  $(\phi = \omega t)$  because we determine the change in  $\epsilon$  with respect to time.

Derivatives:-

$$\therefore \frac{\Delta}{\Delta t} (\cos \omega t) = -\omega \sin \omega t \quad \text{--- (vi)}$$

$$\epsilon = -NBA (-\omega \sin \omega t)$$

$$\epsilon = NBA \omega \sin \omega t$$



$$V = NBA \omega \sin \omega t \quad \text{--- (vii)}$$

When  $\omega t = 90^\circ$

$$V = V_0 (\text{max})$$

$$(vii) \Rightarrow V_0 = NBA \omega \sin (90^\circ)$$



$$V_0 = NAWB \text{ --- (viii)}$$

put eq (viii) in (vii) :

$$V = V_0 \sin \omega t \text{ --- (ix)}$$

~~Star~~ Sinusoidal AC voltage, because it depends on  $\sin \omega t$ .

Dividing b.s of eq ix by R...

$$\frac{V}{R} = \frac{V_0}{R} \sin \omega t$$

$$I = I_0 \sin \omega t$$

Sinusoidal AC Current: vary both in magnitude and direction:

GRAPH:-

$$I = I_0 \sin \omega t$$

(i) when  $\omega t = 0^\circ$

$$I = 0$$

(ii) when  $\omega t = 90^\circ$

$$I = I_0$$

(iii) when  $\omega t = 180^\circ$

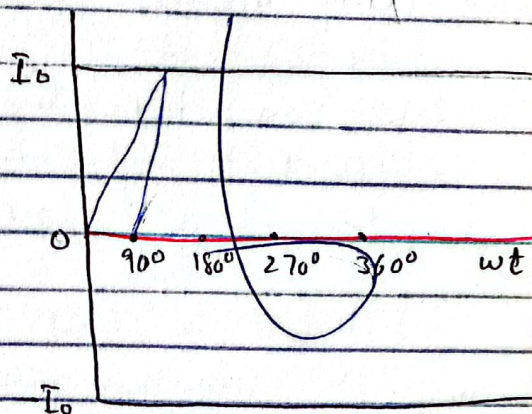
$$I = 0$$

(iv) when  $\omega t = 270^\circ$

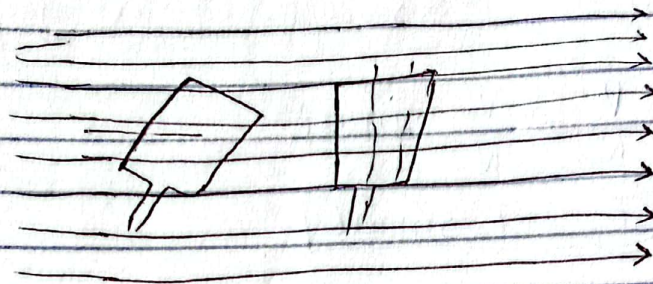
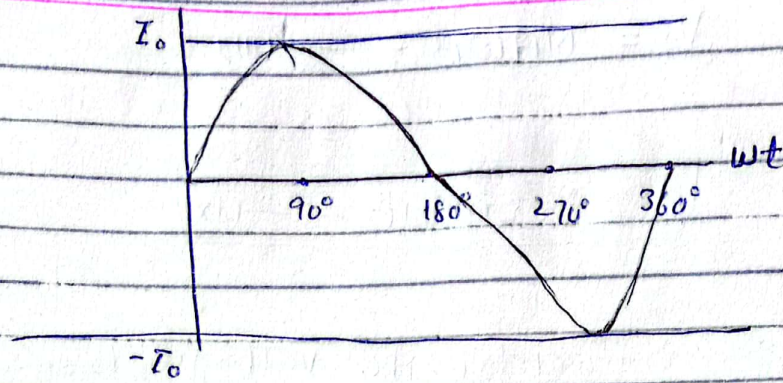
$$I = -I_0$$

(v) when  $\omega t = 360^\circ$

$$I = 0$$







08 Nov 2017

### Eddy Currents :-

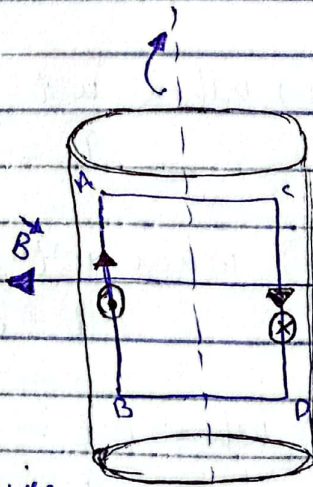
Currents produced in metals due to change of magnetic

flux, when they are moved in magnetic fields are called eddy currents.

\* Eddy means Circulating.

We can determine the direction of current by lenz law.

① If the coil is rotating in clockwise direction - opposing torque will be in Anti-clockwise direction.





D From Side AB;

Magnetic field of current (eddy)

is in out of paper, it is

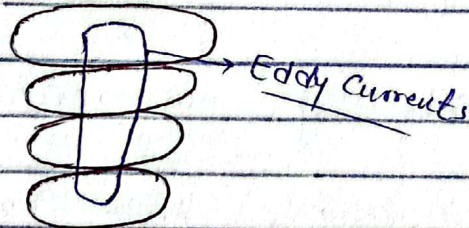
possible when current move from  
BA.

Same rule is applied to another  
side.

\* Energy loss in the metal occurs  
due to eddy currents.

\* Eddy currents can be minimize by

special design.



## AC - MOTOR:

1. Def: A device which converts  
Electrical energy into mechanical  
energy is called AC Motor...

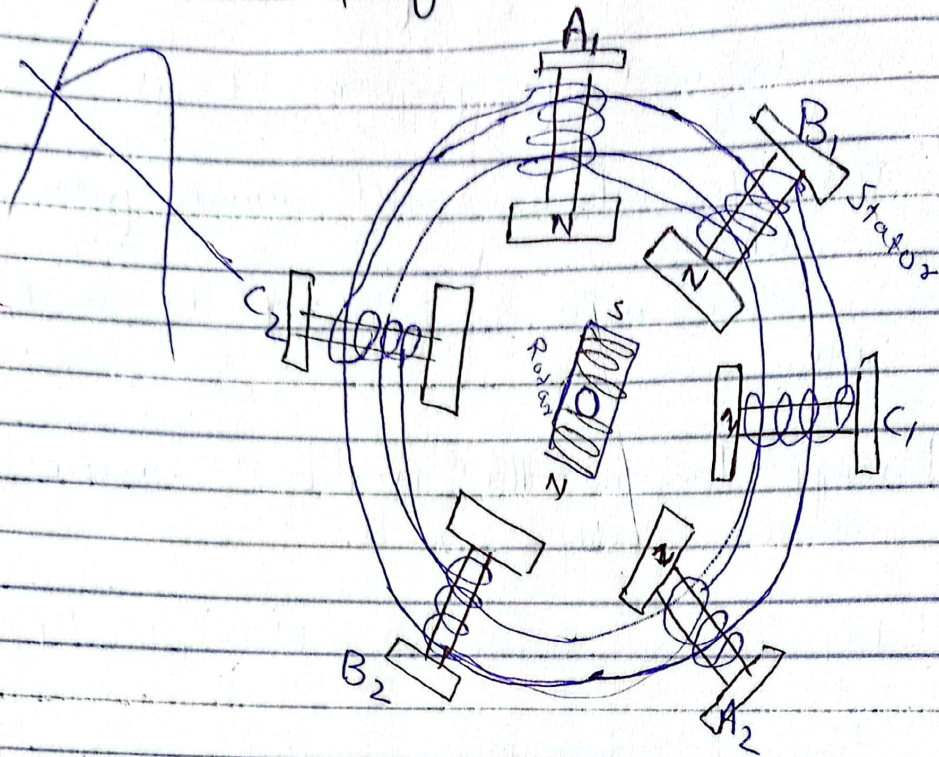
2. principle:- Basic principle of  
AC Motor is Electromagnetic Induction.

3. Construction: Two things;  
(1) Stator:- which is static.



ii) Rotor:- which rotates.

5. Thermal ~~work~~ of work:-



$$B = \mu_0 n I$$

\* Rotating magnetic field is responsible for rotating the rotor.

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Transformer :-

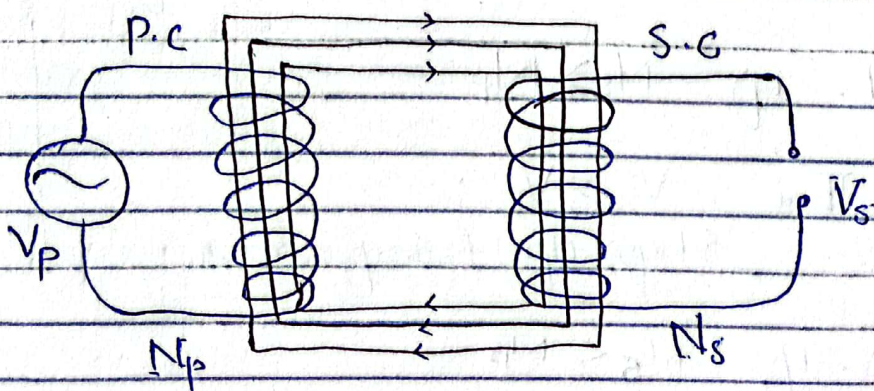
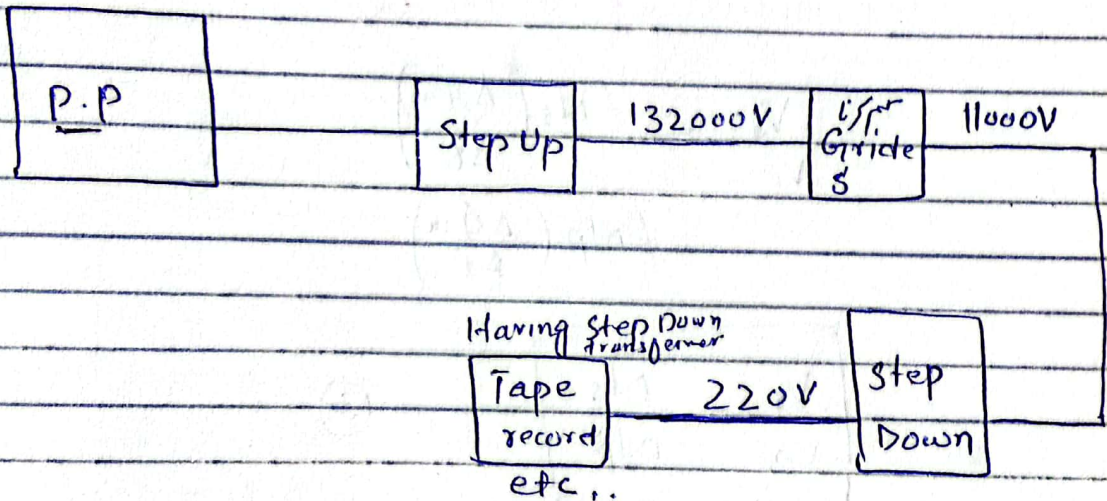
Def: A device which converts Low AC-voltage into high AC-voltage or High AC voltage into low is called transformer.



② principle : Mutual induction...

③ Construction : ① primary coil and secondary coil ② core of transformer.

④ Theory and working





$$\mathcal{E}_s = -N_s \left( \frac{\Delta \Phi_m}{\Delta t} \right)$$

$$V_s = -N_s \left( \frac{\Delta \Phi_m}{\Delta t} \right) \quad \text{--- (1)}$$

$$\mathcal{E}_p = -N_p \left( \frac{\Delta \Phi_m}{\Delta t} \right)$$

When there  
is no resistance  
Induced emf will  
be equal to

$$V_p = -N_p \left( \frac{\Delta \Phi_m}{\Delta t} \right) \quad \text{--- (2)}$$

Divide eq (1) by (2):

$$\frac{V_s}{V_p} = \frac{N_s \left( \frac{\Delta \Phi_m}{\Delta t} \right)}{N_p \left( \frac{\Delta \Phi_m}{\Delta t} \right)}$$

$$\boxed{\frac{V_s}{V_p} = \frac{N_s}{N_p}} \quad \text{--- (3)}$$

Equation of transformer:-

1. If  $N_s > N_p$

Then  $V_s > V_p$

Step up transformer:

2. If  $N_s < N_p$

Then  $V_s < V_p$

Step down transformer: -

$$\frac{20}{10} = \frac{40}{20}$$

Bcz ratio  
is same



For An Ideal transformer:

$$P_{in} = P_{out} \quad (\because P = IV)$$
$$\overset{H}{I}_P \overset{L}{V}_P = \overset{L}{I}_S \overset{H}{V}_S \quad \text{--- (4)}$$

A device which convert low AC voltage and High AC current into High AC voltage and low AC current is called transformer.

$$\frac{V_S}{V_P} = \frac{I_P}{I_S} \quad \text{--- (5)}$$

compare (3) and (4):

$$\frac{I_P}{I_S} = \frac{N_S}{N_P} \quad \text{--- (5)}$$

Ratio b/w currents is equal to inverse ratio of turns....

High voltage = low current....  
low voltage = High current...

Energy losses in transformers:-

1. leakage of flux:- Flux leakage

is responsible for energy loss.



## 2. Resistance of winding:-

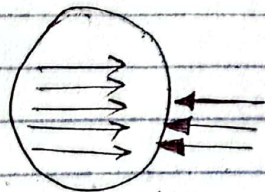
More Resistance = More energy loss and vice versa.

## 3. Eddy Currents:-

Eddy currents are responsible for energy losses in transformers.

## 4. Hysteresis: (Detail in another ch):

Magnetization and demagnetization of iron core occur.  
So some energy is lost in this form...

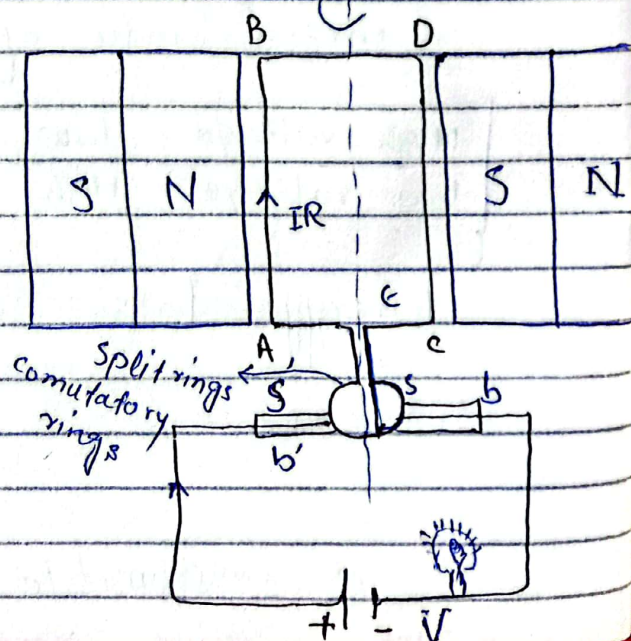


Alignment and disalignment of magnetic lines..

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## Back emf:-

DC Motor





Back emf: oppose the emf of battery

$$V = \epsilon + IR$$

$\leftarrow IR = V - \epsilon$   
It will rotate the  
Coil.

$$\epsilon = \frac{N \Phi}{T}$$

$$I = \frac{V - \epsilon}{R}$$

In Generator,  $\epsilon$  is not back emf

because, we produce emf in  
generator.

\* In Motors, Induced emf is called

back emf because we don't  
want to produce emf, we  
apply emf to motors.

Back

\* Motor effect: when current is  
produced in a coil, this  
current opposes the motion of coil  
this is called <sup>Back</sup> motor effect, in  
generators...



## Capacitor in AC circuit:-

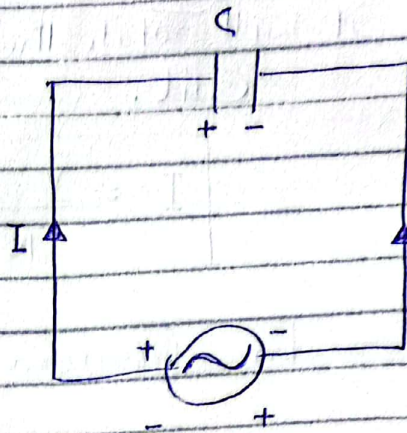
$$V = V_0 \sin \omega t \quad \text{--- (1)}$$

$$Q = CV \quad \text{--- (2)}$$

$$Q = CV_0 \sin \omega t \quad \text{--- (3)}$$

$$I = \frac{\Delta Q}{\Delta t} \quad \text{--- (4)}$$

$$I = \frac{\Delta}{\Delta t} (CV_0 \sin \omega t)$$



$$I = CV_0 \frac{\Delta}{\Delta t} (\sin \omega t) \quad \text{--- (5)}$$

$$\frac{\Delta}{\Delta t} (\sin \omega t) = \omega \cos \omega t \quad \text{--- (6) } \underline{\text{(Derivatives)}}$$

$$I = CV_0 \omega \cos \omega t \quad \text{--- (7)}$$

When  $\omega t = 0^\circ$ ,  $I = I_0$

$$I_0 = CV_0 \omega \cos(0^\circ)$$

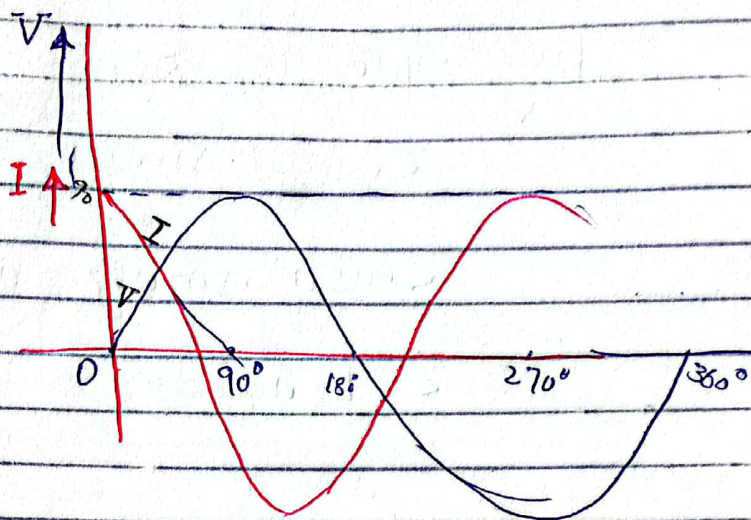
$$I_0 = CV_0 \omega \quad \text{--- (8)}$$

$$I = I_0 \cos \omega t \quad \text{--- (9)}$$

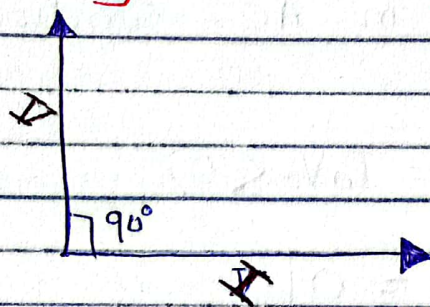
There is a phase difference  
of  $90^\circ$  b/w  $I$  and  $V$



V. They are not in phase.



Phasor Diagram For Capacitor.



Average power dissipated in Capacitor:-

$$\langle P \rangle = \langle IV \rangle \quad \text{--- (I)}$$

$$V = V_0 \sin \omega t$$

$$I = I_0 \cos \omega t$$

$$\langle P \rangle = \langle I_0 \cos \omega t \cdot V_0 \sin \omega t \rangle$$

$$\langle P \rangle = I_0 V_0 \langle \cos \omega t \cdot \sin \omega t \rangle \quad \text{--- (II)}$$

$$\langle \cos \omega t \cdot \sin \omega t \rangle = 0$$

The average value of  $\cos \omega t \sin \omega t = 0$ .



The average value of  $\cos \omega t \cdot \sin \omega t$  per cycle is Zero.

$$\langle \cos \omega t \cdot \sin \omega t \rangle = 0$$

$$\langle \cos 0^\circ \cdot \sin 0^\circ \rangle = 0$$

$$\langle 1 \cdot 0 \rangle = 0$$

$$0 = 0$$

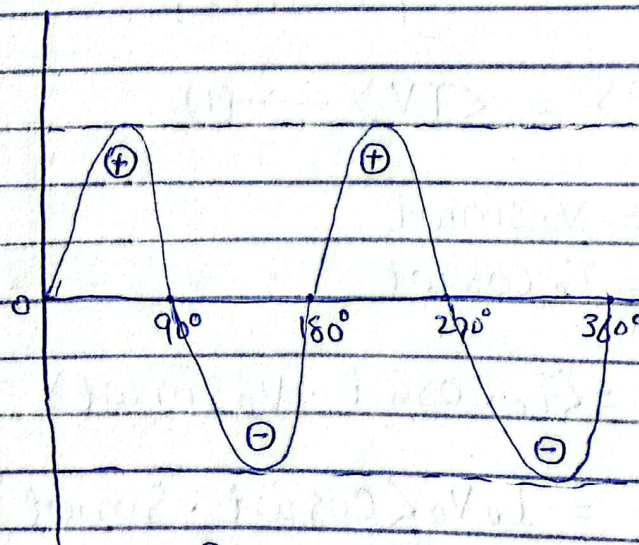
\* Capacitor in DC = Insulator

\* Capacitor in AC = Conductor

$$\langle P \rangle = I_0 V_0 \langle 0 \rangle$$

$$\langle P \rangle = 0$$

Power Wave of Capacitor:



Power Curve.



$$\langle P \rangle = \frac{(+)+(+)+(+)+(-)}{4}$$

$$\langle P \rangle = 0$$

## Reactance of Capacitor / Capacitive Reactance :-

The opposition offered by a Capacitor to the flow of AC current is called Reactance, of capacitor...  
\* Represented by  $X_c$ .

$$V_{rms} = I_{rms} X_c \quad (R = X_c)$$

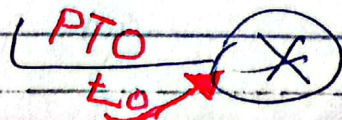
$$X_c = \frac{V_{rms}}{I_{rms}} \quad \text{--- (1)}$$

$$\left. \begin{array}{l} V_{rms} = 0.707 V_0 \\ I_{rms} = 0.707 I_0 \end{array} \right\} \text{--- (2)}$$

put in (1):

$$X_c = \frac{0.707 V_0}{0.707 I_0}$$

$$X_c = \frac{V_0}{I_0} \quad \text{--- (2)}$$



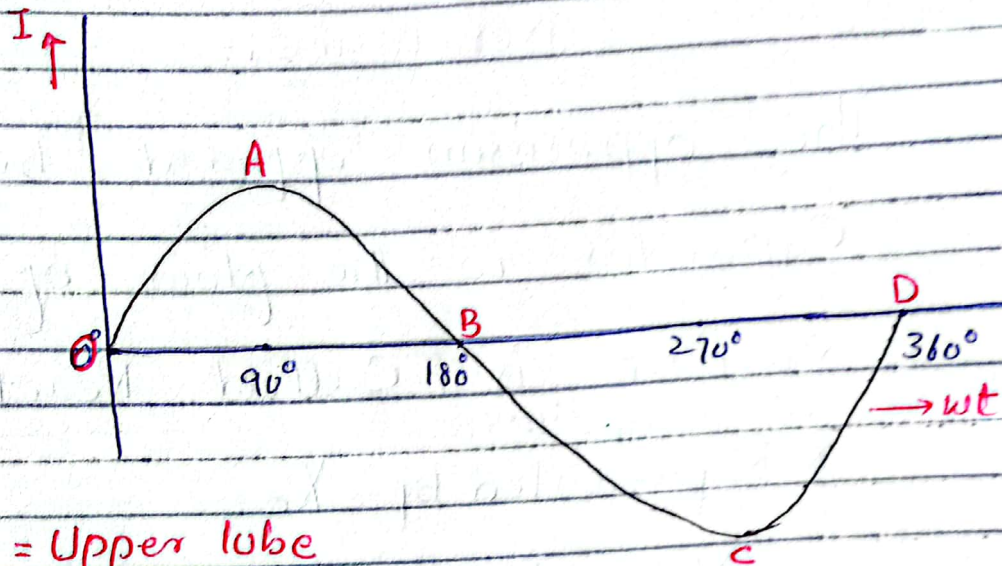


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# Mean, Mean Square and Root mean Square values of A.C Quantities

$$V = V_0 \sin \omega t \quad \text{--- (i) Sinusoidal AC voltage}$$

$$I = I_0 \sin \omega t \quad \text{--- (ii) Sinusoidal AC current}$$



OAB = Upper lobe

BCD = lower lobe

Mean value of AC current is zero:

$$\langle I \rangle = \frac{\text{Area of the lobe OAB} + \text{Area of lobe BCD}}{\lambda}$$

$$\langle I \rangle = 0$$

$$\text{OR } \langle V \rangle = 0$$

Mean power dissipation of AC is not zero.

$$\langle P \rangle = \langle I^2 \rangle R \quad \text{--- (iii)}$$

mean square val

$$\langle P \rangle = \frac{\langle V^2 \rangle}{R} \quad \text{--- (iv)}$$



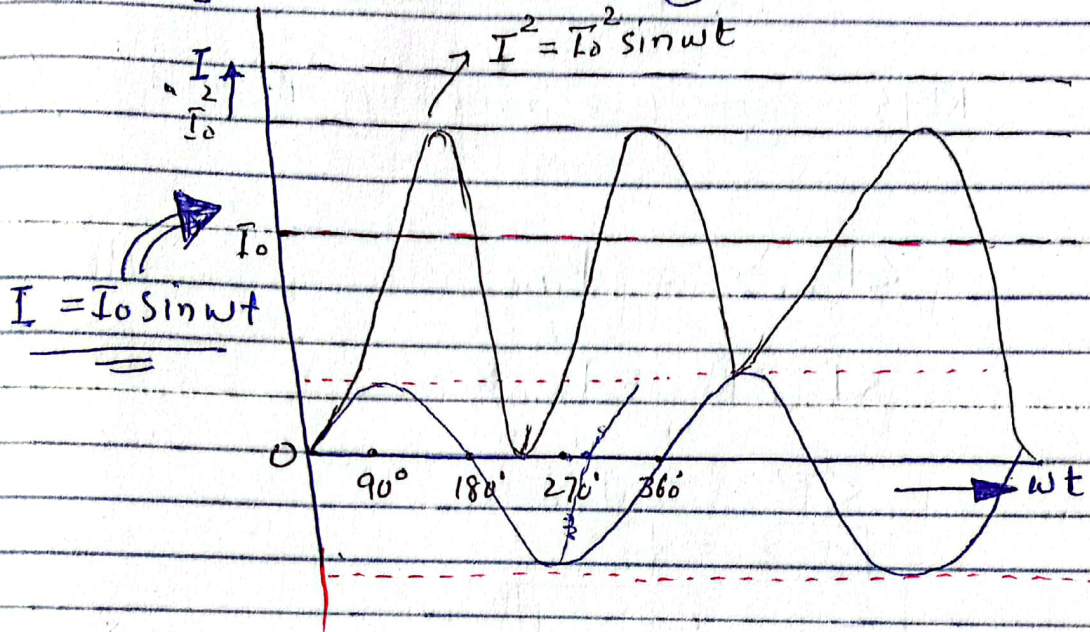
$$\langle I \rangle^2 = \text{Square of mean} = 0$$

$$\langle I^2 \rangle = \text{mean square value} \neq 0$$

Taking Square of (i) and (ii):

$$V^2 = V_0^2 \sin^2 \omega t \quad \text{--- (v)}$$

$$I^2 = I_0^2 \sin^2 \omega t \quad \text{--- (vi)}$$



$$\langle I^2 \rangle = \frac{0 + I_0^2}{2}$$

$$\langle I^2 \rangle = \frac{I_0^2}{2} \neq 0$$

Mean square value of AC is not zero.

$$\langle I^2 \rangle = \frac{I_0^2}{2}$$

Taking Square Root of b.s:

$$\sqrt{\langle I^2 \rangle} = \sqrt{\frac{I_0^2}{2}}$$

$$I_{\text{rms}} = \frac{I_0}{\sqrt{2}}$$

$$I_{\text{rms}} = 0.707 I_0$$



$$\frac{\sin^2 \phi - (\sin \phi)^2}{\sin^2 \phi} \pm$$

$$V_{rms} = 0.707 V_0$$

$I_{rms}$  a little bit greater than

$I$

RMS = effective value of AC voltage/current

$$\langle P_{a.c.} \rangle = P_{d.c.}$$

$$\langle I^2 \rangle R = I_{d.c.}^2 R$$

$$\langle I^2 \rangle = I_{d.c.}^2$$

$$\sqrt{\langle I^2 \rangle} = \sqrt{I_{d.c.}^2}$$

$$I_{rms} = I_{d.c.}$$

$I_{rms}$  = effective value of AC.

$$I_{rms} = \dots$$

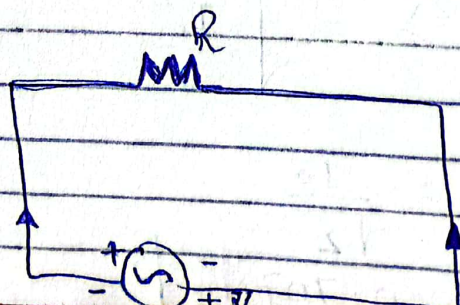
15 NOV 2017

Single element A.C. Circuits:-

Having only one circuit element. (Capacitor, R or inductor).

① Resistor in A.C. circuit:- OR

(AC through Resistor):-



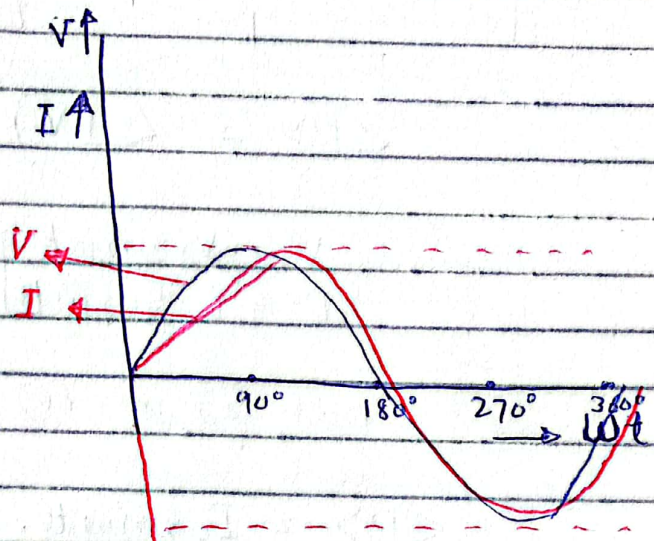


$$V = V_0 \sin \omega t \quad \text{--- (1)}$$

Dividing eq (1) by R.

$$\frac{V}{R} = \frac{V_0}{R} \sin \omega t$$

$$I = I_0 \sin \omega t \quad \text{--- (2)}$$



\* In Resistor (in AC circuit)

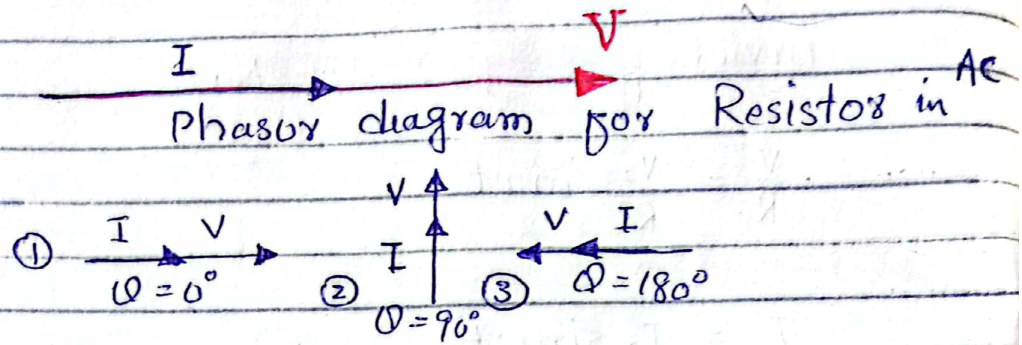
There is no phase difference in voltage and current because they are in phase.

Phase difference is zero;

\* V and I are called phasors.  
Because they vary with phase angle. →

\* AC voltage and current are also called rotating vectors...





**Average power dissipated in Resistor**

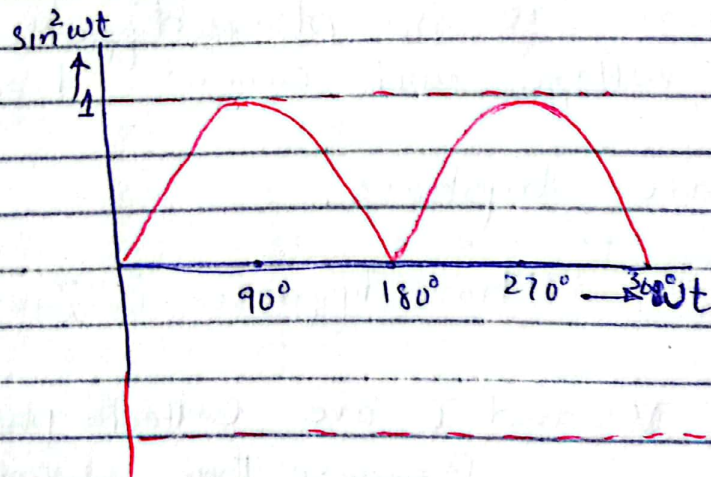
$$\langle P \rangle = \langle IV \rangle \text{ --- (1)}$$

$$\left. \begin{aligned} V &= V_0 \sin \omega t \\ I &= I_0 \sin \omega t \end{aligned} \right\} \text{ --- (2)}$$

put (2) in (1).

$$\langle P \rangle = I_0 \sin \omega t \cdot V_0 \sin \omega t$$

$$\langle P \rangle = I_0 V_0 \langle \sin^2 \omega t \rangle \text{ --- (3)}$$



$$\langle \sin^2 \omega t \rangle = \frac{0 + 1}{2}$$

$$\langle \sin^2 \omega t \rangle = \frac{1}{2} \text{ --- (4)}$$



Put eq (4) in eq (3):

$$\langle P \rangle = I_0 V_0 \times \frac{1}{2}$$

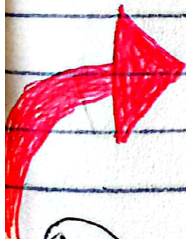
$$= \frac{I_0 V_0}{\sqrt{2} \times \sqrt{2}}$$

$$= 0.707 I_0 \times 0.707 V_0$$

$$\langle P \rangle = I_{rms} V_{rms}$$

$\langle P \rangle$  = effective value of  $I$   $\times$  effective value of  $V$ .

In Resistor AC and AV are in phase, so power dissipation will take place...

  $I = I_0 \cos \omega t$  — (x)

$$V = C V_0 \omega \cos \omega t$$
 — (y)



~~For~~ Comparing x and y,

$$I_0 \cos \omega t = C V_0 \omega \cos \omega t$$

$$I_0 = C V_0 \omega$$
 — (3)

Put in (2)  $\Rightarrow X_c = \frac{V_0}{I_0}$

$$X_c = \frac{V_0}{C V_0 \omega}$$



$$X_c = \frac{1}{\omega c} \quad \text{--- (4)}$$

$$\therefore \omega = \frac{2\pi}{T}$$

$$\omega = 2\pi f$$

$$X_c = \frac{1}{2\pi f c}$$

$$X_c \propto \frac{1}{f}$$

(R)  
Difference b/w Resistance and  
Reactance is that:  
( $X_c$ )

\* Resistor does not depend upon frequency.

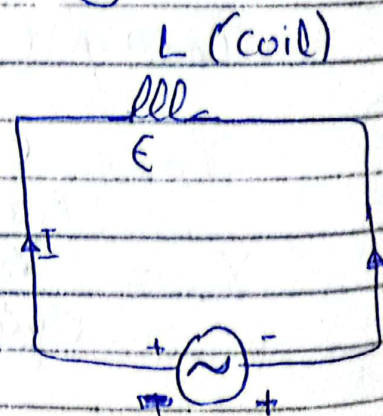
\* Reactance depends upon frequency

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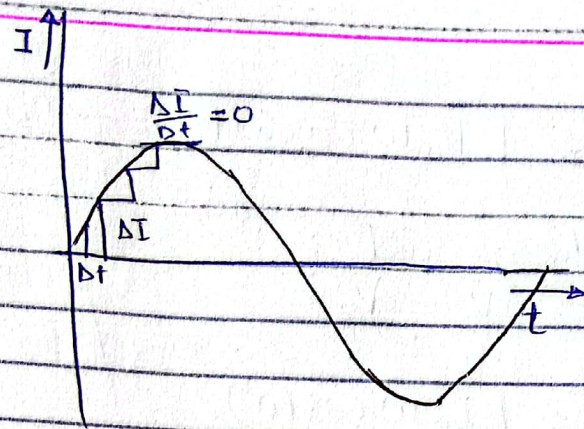
Inductor in AC Circuit:-

$$I = I_0 \sin \omega t \quad \text{--- (1)}$$

A Coil with negligible resistance and Large Inductance. Self Induction is called Inductor.







$$\epsilon = L \left( \frac{\Delta I}{\Delta t} \right)$$

At start current is minimum, but

$\left( \frac{\Delta I}{\Delta t} \right)$  is large (maximum) i.e

Induced emf is maximum.

\* In Inductance the voltage is leading the current.

$$\epsilon = L \left( \frac{\Delta I}{\Delta t} \right)$$

$$V = L \left( \frac{\Delta I}{\Delta t} \right) \quad \text{--- (2)}$$

put (2) in (1):

$$V = L \frac{\Delta}{\Delta t} (I_0 \sin \omega t)$$

$$V = LI_0 \frac{\Delta}{\Delta t} (\sin \omega t)$$

$$\therefore \frac{\Delta}{\Delta t} (\sin \omega t) = \omega \cos \omega t$$

Derivatives



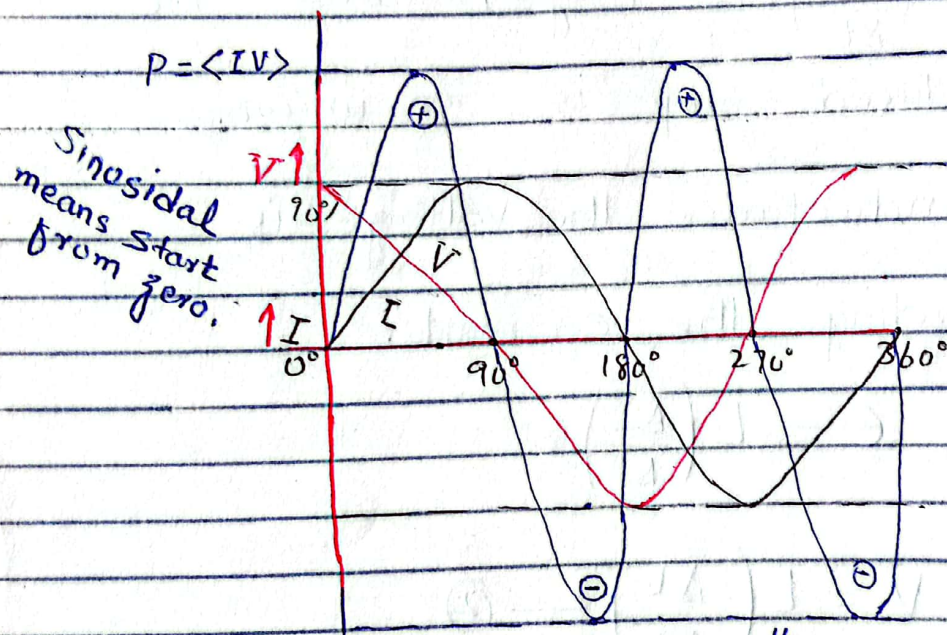
$$V = LI_0 \omega \cos \omega t \quad \text{--- (5)}$$

When  $\omega t = 0^\circ$   
 $V = V_0$

$$V_0 = LI_0 \omega \cos(0^\circ)$$

$$V_0 = LI_0 \omega \quad \text{--- (6)}$$

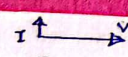
$$V = V_0 \cos \omega t \quad \text{--- (7)}$$

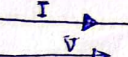


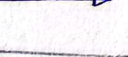
It is clear from the graph that in inductor, the voltage is ~~back~~ leading the current by an angle of  $90^\circ$ .

\* There is phase difference.

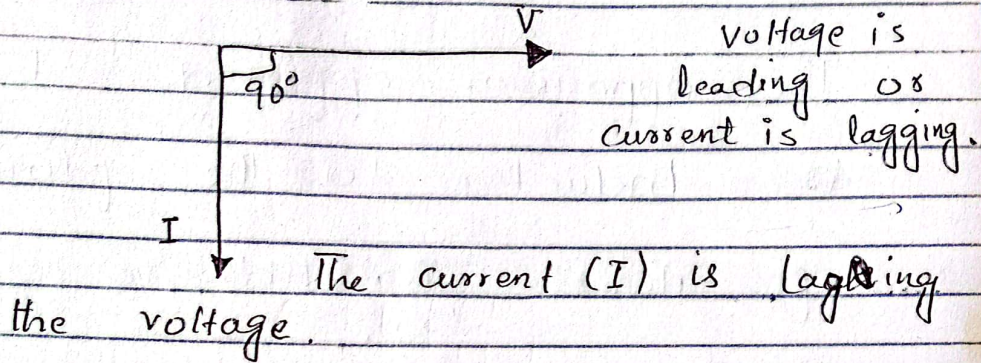


Capacitor :- 

Resistor :- 

Inductor :- 

### Phasor Diagram for Inductor:



### Average power loss in Inductor:-

$$\langle P \rangle = \langle I V \rangle$$

In Inductor:

$$I = I_0 \sin \omega t$$

$$V = V_0 \cos \omega t$$

$$\langle P \rangle = \langle I_0 \sin \omega t \cdot V_0 \cos \omega t \rangle$$

$$\langle P \rangle = I_0 V_0 \langle \sin \omega t \cdot \cos \omega t \rangle$$

$$\langle P \rangle = I_0 V_0 \langle 0 \rangle$$

$$\boxed{\langle P \rangle = 0}$$

\* Inductor store energy in Magnetic field.

Capacitor:  $u = \frac{1}{2} \epsilon E^2$



## Reactance of Inductor (Inductive Reactance):-

The opposition offered by an inductor to the flow of AC, is called inductive reactance " $X_L$ ".

$$V_{rms} = I_{rms} X_L \quad (R = X_L)$$

$$X_L = \frac{V_{rms}}{I_{rms}} \quad \text{--- (1)}$$

$$X_L = \frac{0.707 V_0}{0.707 I_0}$$

$$X_L = \frac{V_0}{I_0} \quad \text{--- (2)}$$

$$\begin{aligned} V &= V_0 \cos \omega t \\ V &= L \omega I_0 \cos \omega t \end{aligned} \quad \left. \begin{array}{l} \uparrow \\ \uparrow \end{array} \right\} \text{Compare them}$$
$$V_0 \cos \omega t = L \omega I_0 \cos \omega t$$

$$V_0 = L \omega I_0 \quad \text{--- (3)}$$

$$X_L = \frac{L \omega I_0}{I_0}$$

$$X_L = L \omega$$
$$\omega = 2\pi f$$



$$X_L = 2\pi fL \quad X_C = \frac{1}{\omega C} = \frac{1}{2\pi fC}$$

Inductor and capacitor are inverse of each other.

When we apply DC to capacitor:

In case of DC, Inductive Reactance

( $X_L$ ) is zero...

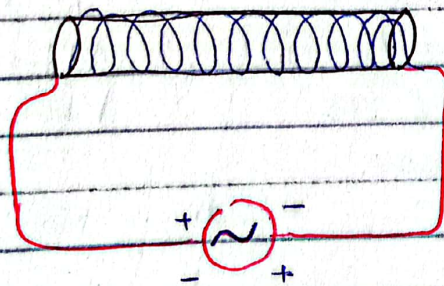
In case of DC, Capacitive reactance has infinite value...

Inductive choke:-

It is an arrangement

in which a copper wire is wound upon an iron core such that it

supplies a constant AC to a circuit without any energy loss.



$$B = \mu_r \mu_0 I$$

$$M_m = \frac{1}{2} \frac{B^2}{\mu}$$



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## Impedance - ( $Z$ )

The combined opposition offered by Resistor, Capacitor and Inductor to the flow of AC is called Impedance.

$$V_{rms} = I_{rms} Z \quad (R = Z \text{ (Impedance)})$$

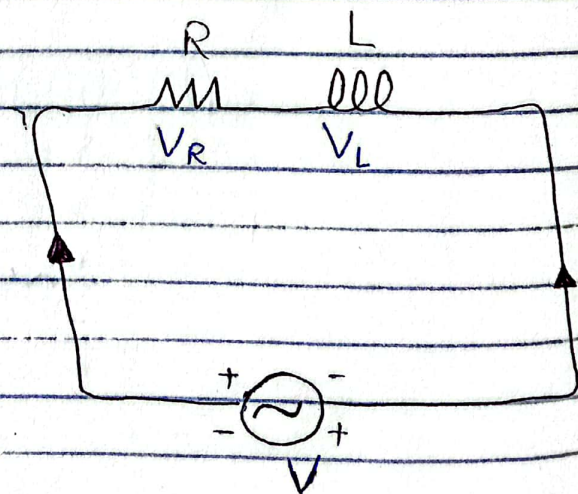
$$Z = \frac{V_{rms}}{I_{rms}}$$

$$Z = \text{ohm}$$

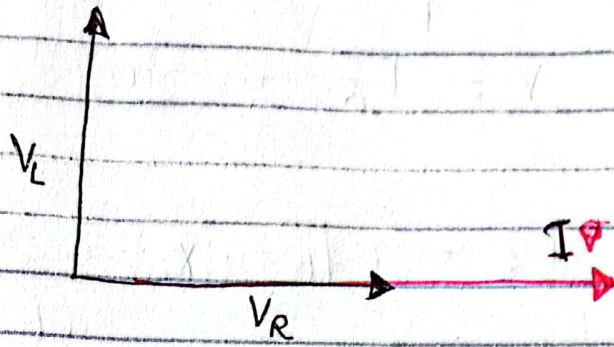
\* Dimensionally  $X_L$ ,  $X_C$  and  $R$  having same unit (ohm).

## RL Series AC Circuit :-

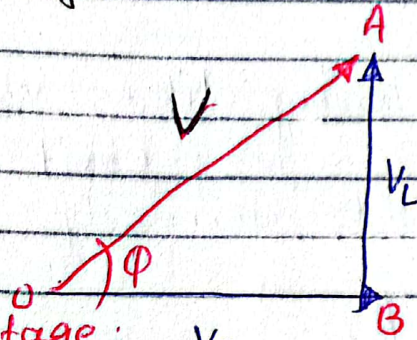
\* Current in Series remains constant, so we take  $I$  as reference phasor.







By Adding:  $v = V_R + V_L$



① Applied voltage:  $V_R$   
 In  $\Delta OAB$ : By Pythagorean theorem;

$$(OA)^2 = (OB)^2 + (AB)^2$$

$$V^2 = (V_R)^2 + (V_L)^2 \quad \text{--- ①}$$

$$\left. \begin{array}{l} \because V_R = IR \\ V_L = IX_L \end{array} \right\} \text{--- ②}$$

Put ② in ①:

$$V^2 = (IR)^2 + (IX_L)^2$$

$$V^2 = I^2 R^2 + I^2 X_L^2$$

$$V^2 = I^2 (R^2 + X_L^2)$$

$$\boxed{V = I \sqrt{R^2 + X_L^2}} \quad \text{--- ③ Applied voltage.}$$



## ② Impedance:-

$$V = IR \quad \text{--- (4)}$$

$$IZ = I\sqrt{R^2 + X_L^2}$$

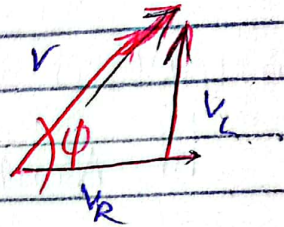
$$Z = \sqrt{R^2 + X_L^2} \quad \text{--- (5)}$$

$$|A| = \sqrt{A_x^2 + A_y^2}$$

Impedance.

Z, is behaving like vector, that's why we can't determine it directly by  $Z \neq R + X_L$

## ③ Angle ( $\phi$ ) :-



$$\tan \phi = \frac{V_L}{V_R}$$

$$\phi = \tan^{-1} \left( \frac{V_L}{V_R} \right) \quad \text{--- (6)}$$

$$\phi = \tan^{-1} \left( \frac{IX_L}{IR} \right)$$

$$\phi = \tan^{-1} \left( \frac{X_L}{R} \right) \quad \text{--- (7)}$$

## ④ power factor:-

$$\cos \phi = \frac{V_R}{V} \quad \text{--- (8)}$$

$$\cos \phi = \frac{IR}{IZ}$$



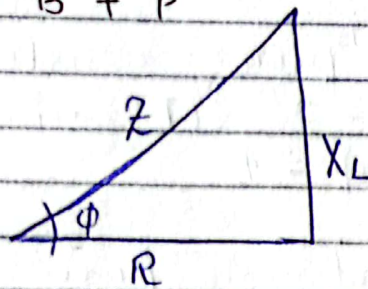
$$\frac{V}{I} = Z = \frac{V}{I}$$

$$\cos \phi = \frac{R}{Z} \quad \text{--- (9)}$$

From eq (5) we can draw Impedance triangle...

$$Z = \sqrt{R^2 + X_L^2}$$

$$H = B + P$$



We can calculate:

(i)  $Z$  (Impedance)

(ii)  $\phi$  (Angle (phase angle))

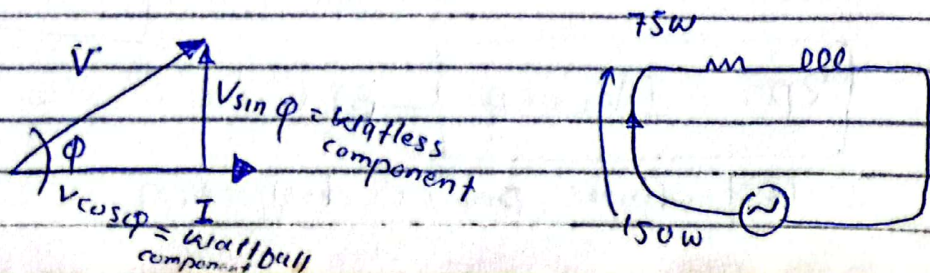
(iii)  $\cos \phi$  (Power Factor) from Impedance triangle...

$$\cos \phi = R/Z$$

Power Factor:-

It is ratio of same quantities, having no unit.

$$P.F = \frac{\text{Power dissipation}}{\text{power supplied}}$$





$$P.F = \frac{IV \cos \phi}{IV}$$

$$P.F = \cos \phi$$

$\cos \phi$  is a dimensionless number...

$\therefore$  If circuit is pure resistive circuit.  
 $\phi = 0^\circ$  (I and V are in phase)  
 $\cos \phi = 1$

$\therefore$  If circuit is pure inductive/capacitive  
 $\phi = 90^\circ$  (I and V are out of phase)  
 $\cos(90^\circ) = 0$   $\cos \phi = 0$

20 Nov 2017  
 Power dissipation in RL series AC circuit :-

$$\langle P \rangle = I_{rms} V_{rms} \cos \phi$$

$$\langle P \rangle = \frac{I_0 V_0}{2} \cos \phi$$

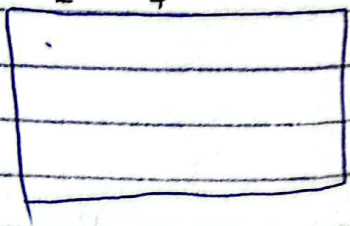
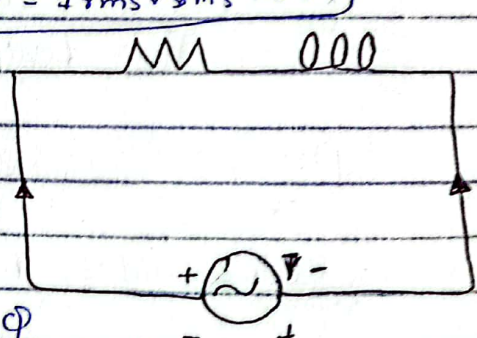
$$= \frac{I_0}{\sqrt{2}} \times \frac{V_0}{\sqrt{2}} \cos \phi$$

$$= 0.707 I_0 \times 0.707 V_0 \cos \phi$$

$$\langle P \rangle = I_{rms} \cdot V_{rms} \cos \phi \quad \text{--- (1)}$$

$$\langle P \rangle = IV \cos \phi \quad \text{--- (2)}$$

Instantaneous power dissipation...





As

$$V = IZ$$

$$\cos \phi = \frac{\text{Base}}{\text{Hypotenous}}$$

$$\cos \phi = \frac{R}{Z}$$

put these values in eq. (2):

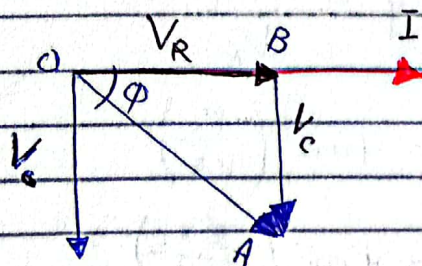
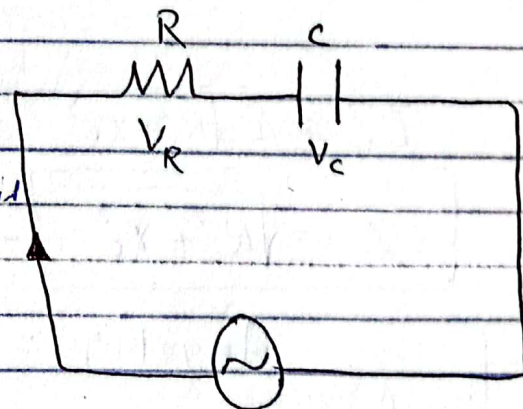
$$\langle P \rangle = I(IZ) \frac{R}{Z}$$

$$\langle P \rangle = I^2 R$$

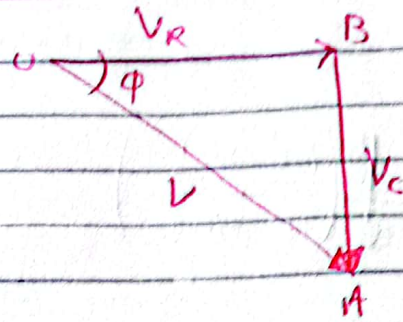
It shows that the power is dissipated by resistor in RL Series Circuit.

### RC Series AC circuits:-

In RC Series the voltage lags behind the current by angle  $\phi$ .







In  $\Delta OAB$ :

$$V^2 = V_R^2 + V_C^2 \quad \text{--- (1)}$$

$$V_R = IR$$

$$V_C = I X_C$$

$$\Rightarrow V^2 = \sqrt{(IR)^2 + (IX_C)^2}$$

$$V = I \sqrt{R^2 + X_C^2} \quad \text{--- (2)}$$

$$V = IZ$$

$$IZ = I \sqrt{R^2 + X_C^2}$$

$$Z = \sqrt{R^2 + X_C^2} \quad \text{--- (3)}$$

Angle ( $\phi$ ):-

In  $\Delta OAB$ ,

$$\tan \phi = \frac{V_C}{V_R}$$

$$\phi = \tan^{-1} \left( \frac{V_C}{V_R} \right)$$

$$\phi = \tan^{-1} \left( \frac{IX_C}{IR} \right)$$



$$\phi = \tan^{-1} \left( \frac{X_c}{R} \right) \text{ --- (4)}$$

power factor:-

$$\cos \phi = \frac{V_R}{V}$$

$$\cos \phi = \frac{I_R}{I_Z}$$

$$\cos \phi = \frac{R}{Z} \text{ --- (5)}$$

Impedance triangle..

We can calculate

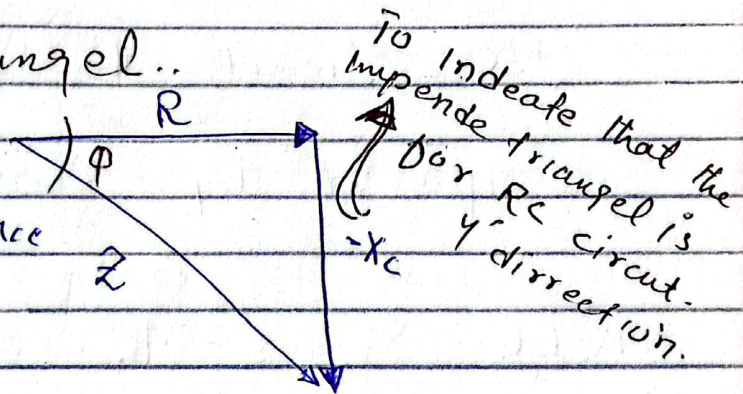
from the Impedance triangle.



(i) Z

(ii)  $\tan \phi$  or Simple  $\phi$  (Phase angle).

(iii)  $\cos \phi$  (Power Factor).



Average power dissipation in

RC circuit:-

$$\langle P \rangle = \frac{I_0 V_0}{2} \cos \phi$$

$$\langle P \rangle = I_0 \times \frac{V_0}{\sqrt{2}} \cos \phi$$

$$\langle P \rangle = I_{rms} \cdot V_{rms} \cos \phi$$



$$\langle P \rangle = IV \cos \phi \quad \text{--- (1)}$$

$$V = IR$$

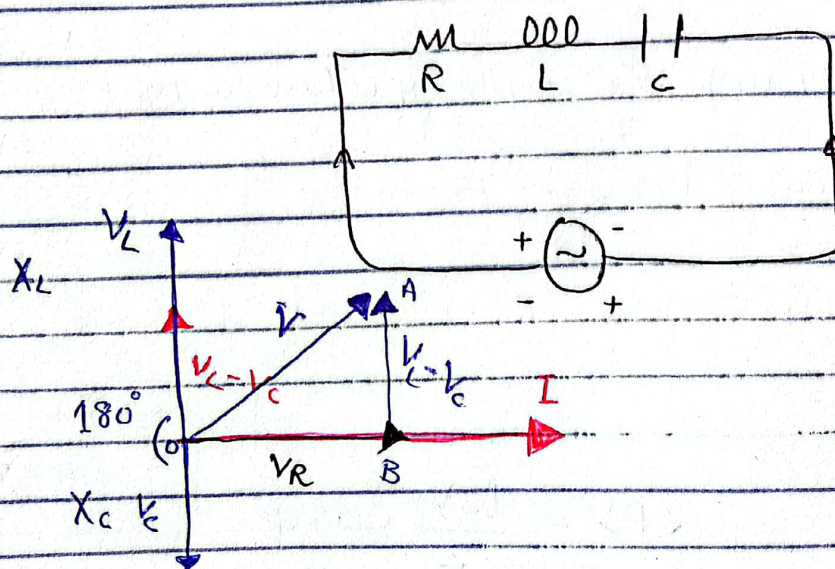
Put in (1):

$$\Rightarrow \langle P \rangle = I(I R) \left( \frac{R}{R} \right)$$

$$\Rightarrow \langle P \rangle = I^2 R$$

which also shows that in RC circuit the power is dissipated by Resistor....

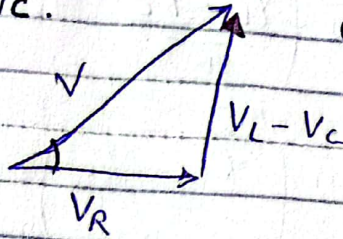
### RLC Series AC Circuit:



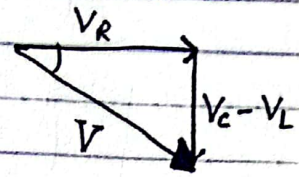
\* Voltage across inductor and capacitor in RLC circuit are out of phase by an angle of  $180^\circ$ .



① when  $V_L > V_C$ .



② when  $V_C > V_L$



$$V^2 = V_R^2 + (V_L - V_C)^2 \quad \text{--- (1)}$$

$$V = IR$$

$$V_L = IX_L$$

$$V_C = IX_C$$

$$V^2 = V_R^2 + (IX_L - IX_C)^2$$

$$V = I \sqrt{R^2 + (X_L - X_C)^2}$$

$$V = I \sqrt{R^2 + (X_L - X_C)^2} \quad \text{--- (2)}$$

$$V = IZ$$

$$IZ = I \sqrt{R^2 + (X_L - X_C)^2}$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2} \quad \text{--- (3)}$$

$$\tan \phi = \frac{V_L - V_C}{V_R}$$

$$\phi = \tan^{-1} \left( \frac{V_L - V_C}{IR} \right) \quad \text{--- (4)}$$

$$\phi = \tan^{-1} \left( \frac{IX_L - IX_C}{IR} \right)$$



$$\phi = \tan^{-1} \left( \frac{X_L - X_C}{R} \right)$$

$$\phi = \tan^{-1} \left( \frac{X_L - X_C}{R} \right) \quad \text{--- 6}$$

Power Factor:-

$$\cos \phi = \frac{V_R}{V}$$

$$\cos \phi = \frac{IR}{IZ}$$

$$\cos \phi = R/Z \quad \text{--- 7}$$

Impedance triangle:-

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$



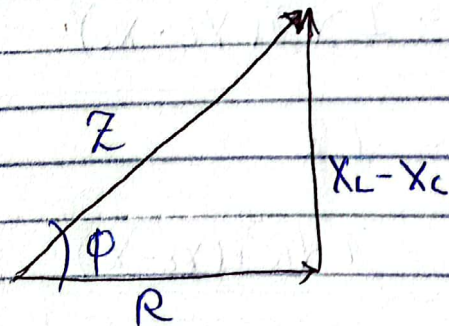
①  $X_L > X_C \Rightarrow$

②  $X_C < X_C$

③  $X_L = X_C$

④  $X_L - X_C \geq 0$

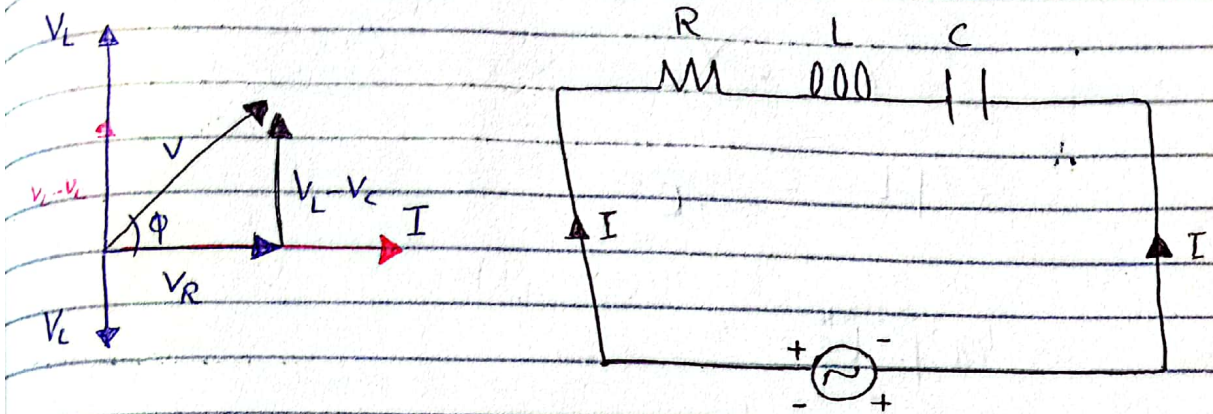
⑤  $X_L - X_C < 0$  means  $X_L$  is less than  $X_C$ .





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## RLC - Series Resonance A.C Circuit:



As we know that:

$$Z = \sqrt{R^2 + (X_L - X_C)^2} \quad \text{--- (I)}$$

$$Z = IV$$

$$I = \frac{V}{Z} \quad \text{--- (II)}$$

As we know that:

$$X_L = 2\pi fL$$

$$X_C = \frac{1}{2\pi fC}$$

When we increase  $f$ ,  $X_L$  increases and

$X_C$  decreases, at a

particular frequency

$X_L = X_C$  This frequency

is called resonance frequency.

$X_L$	$X_C$
0	10
1	9
2	8
3	7
4	6
5	5
6	4
7	3
8	2
9	1
10	0



$\therefore$  When  $f = f_0$   $\rightarrow$  Resonance frequency

$$X_L = X_C$$

$$2\pi f_0 L = \frac{1}{2\pi f_0 C}$$

$$4\pi^2 f_0^2 LC = 1$$

$$f_0^2 = \frac{1}{4\pi^2 LC}$$

$$f_0 = \frac{1}{2\pi \sqrt{LC}}$$

When Resonance takes place,  
i.e.  $X_L = X_C$

$$\text{and } X_L - X_C = 0$$

$$\text{eg } \textcircled{1} \Rightarrow Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$Z = R$$

When Resonance takes place Circuit

becomes resistive,

\* When Resonance takes place  
Impedance becomes minimum

and Current becomes maximum.

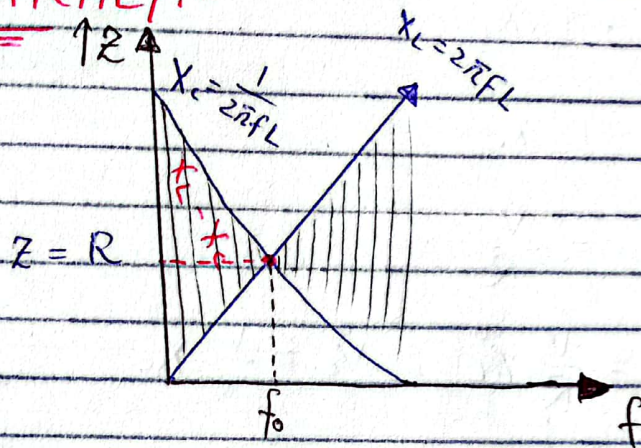
$$\text{eg } \textcircled{2} \Rightarrow I = \frac{V}{Z}$$

$$I_0 = \frac{V}{R} \quad \textcircled{3}$$

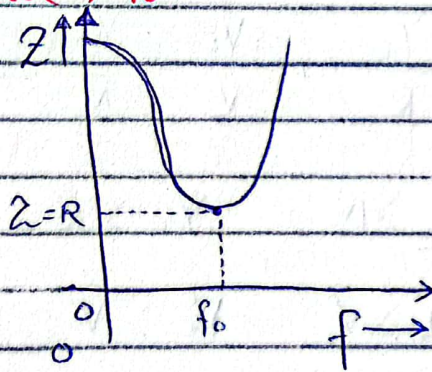


The frequency at which Current becomes maximum, or Impedance become minimum is called Resonance frequency.

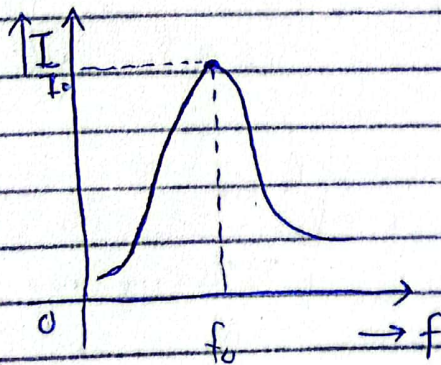
GRAPHICALLY:-



For Impedance,  $Z$ :



For Current,  $I$ :





When Resonance take place,

• Voltage across Inductor is

equal to voltage across resistor.

$$\dot{V}_L = \dot{V}_C$$

$$\dot{V}_L = \dot{I}_0 X_L$$

$$\dot{V}_C = \dot{I}_0 X_C$$

$$\text{As } \dot{I}_0 = \frac{V}{R}$$

$$\dot{V}_L = \frac{V}{R} X_L, \quad \dot{V}_C = \frac{V}{R} X_C$$

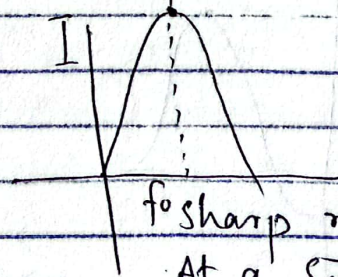
$$\frac{\dot{V}_L}{V} = \left( \frac{X_L}{R} \right), \quad \frac{\dot{V}_C}{V} = \left( \frac{X_C}{R} \right) \rightarrow \text{Quality Factor.}$$

$$\therefore X_L > R, \quad X_C > R$$

$$\dot{V}_L > V, \quad \dot{V}_C > V$$

$$\frac{\dot{V}_L}{V} = Q \text{ (Quality Factor).}$$

$$\frac{\dot{V}_C}{V} = Q$$



$f_0$  sharp resonance

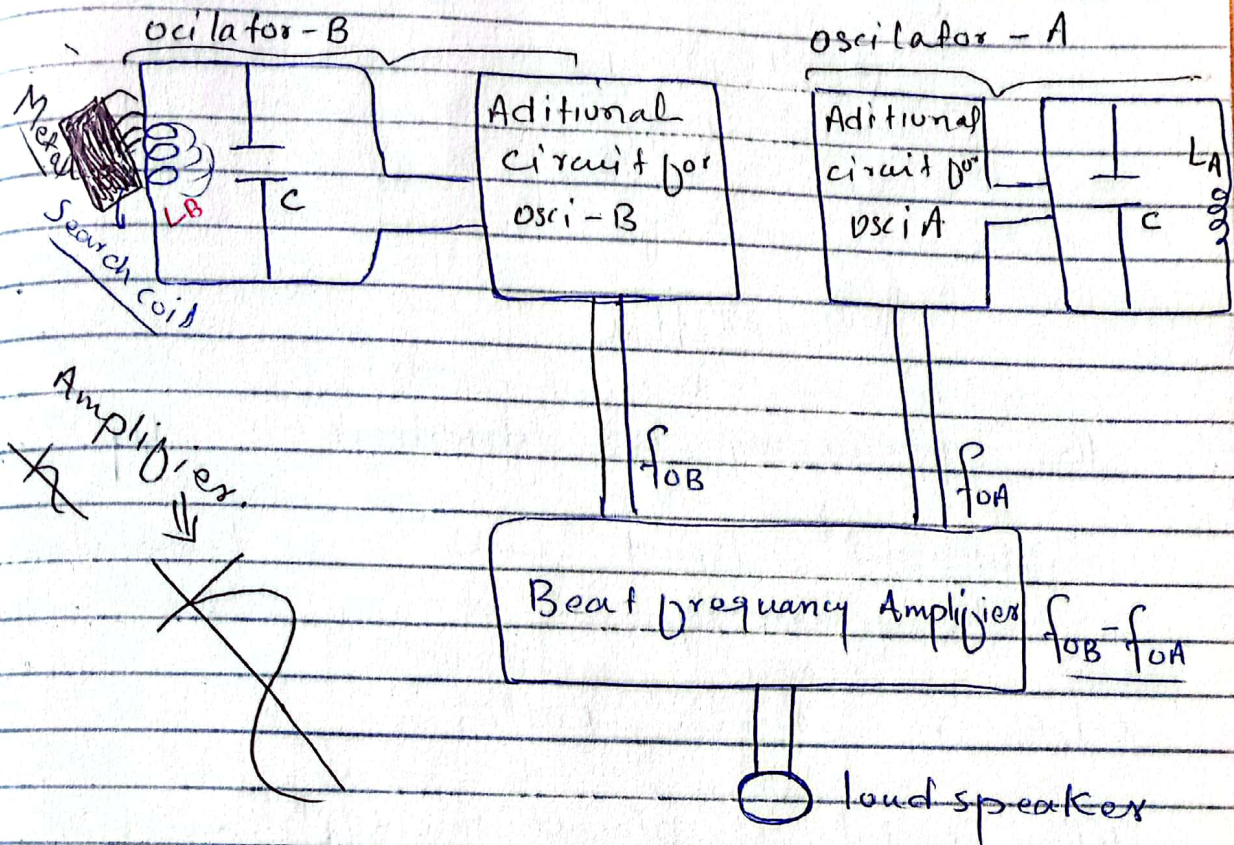
At a single value of

frequency resonance takes place



22 NOV 2017

## principle of Metal Detectors:



\* Devices by which metals are detected.

\* Energy oscillate b/w two points in LC circuit.

\* Energy oscillate b/w Inductor and Capacitor. i.e Between Magnetic energy and electric energy.

\* This Oscillators have Specific frequency, i.e (No. of vibration b/w L and C.

The



This frequency is given by:

$$f_{0A} = \frac{1}{2\pi} \sqrt{\frac{1}{LC}}$$

$$f_{0B} = \frac{1}{2\pi} \sqrt{\frac{1}{L_B C}}$$

This frequency is absorbed by

Additional circuit and is transferred to frequency

\*  $L_B$  is Search coil.

When metal is placed in its magnetic field, it changes magnetic flux.

or leakage of magnetic flux, so

$L_B$  (self induction) decreases

and hence  $f_{0B}$  increases, thus

$f_{0B} - f_{0A}$  increases  $\rightarrow$  loud speaker will produce sound.

Maximum power transfer:- or  
Maximum power transfer theorem:-

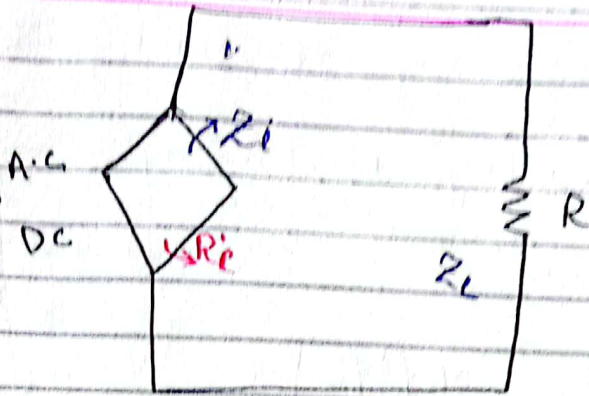


In case of DC:-

When  $R_i = R$

The Battery will

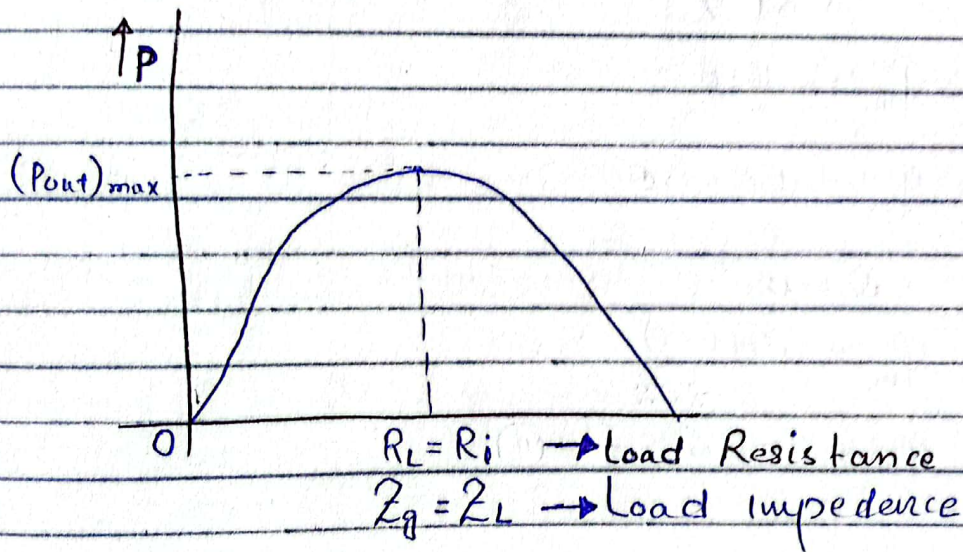
provide maximum or  
power to circuit



$Z_i$  or  $Z_g \rightarrow$  Impedance of generator

When  $Z_g, Z_i = Z_L$

The source will provide maximum  
power to the load.



23 NOV 2017

Maxwell's Equations (Electromagnetic waves):

(b) Changing magnetic field (magnetic flux) produces Electric field.

(a) Changing Electric field (electric flux)



Maxwell's

↑  
produces magnetic field.

According to Faraday

law:

$$\mathcal{E} = -N \left( \frac{\Delta \Phi_m}{\Delta t} \right)$$

$$N = 1$$

$$\mathcal{E} = - \left( \frac{\Delta \Phi_m}{\Delta t} \right)$$

$$V = - \left( \frac{\Delta \Phi_m}{\Delta t} \right) \quad \text{--- (i)}$$

$$\Phi_m = \vec{B} \cdot \vec{A}$$

$$\Phi_m = BA \cos \theta$$

$$\theta = 180^\circ$$

$$\Phi_m = BA(-1)$$

$$\Phi_m = -BA \quad \text{--- (ii)}$$

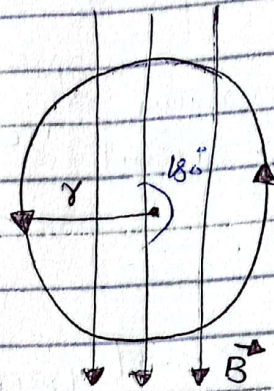
put eq (ii) in (i).

$$V = - \frac{\Delta}{\Delta t} (-BA)$$

$$V = A \frac{\Delta B}{\Delta t} \quad \text{--- (iii)} \quad \left( \because A \text{ is constant} \right)$$

We know that:

$$V = \frac{W}{q} \quad \text{--- (iv)}$$





$$W = \vec{F}_e \cdot \vec{d}$$

$$W = F_e d \cos \theta$$

$$W = F_e d \cos(0^\circ)$$

$$W = F_e d \quad \text{--- (V)}$$

$$\cos(0^\circ) = 1$$

$$F_e = qE$$

$$d = 2\pi r$$

$$\Rightarrow W = qE(2\pi r) \quad \text{--- (VI)}$$

Put eq (VI) in (IV)

$$V = \frac{qE(2\pi r)}{q}$$

$$V = E(2\pi r) \quad \text{--- (VII)}$$

Equate (III) and (VII):

$$E(2\pi r) = A \left( \frac{\Delta B}{\Delta t} \right)$$

$$E = \frac{A}{2\pi r} \left( \frac{\Delta B}{\Delta t} \right)$$

$$E = \frac{1}{2\pi r} \left( \frac{\Delta \Phi_m}{\Delta t} \right)$$

Maxwell 1<sup>st</sup> equation

Whenever you change B there will be E.



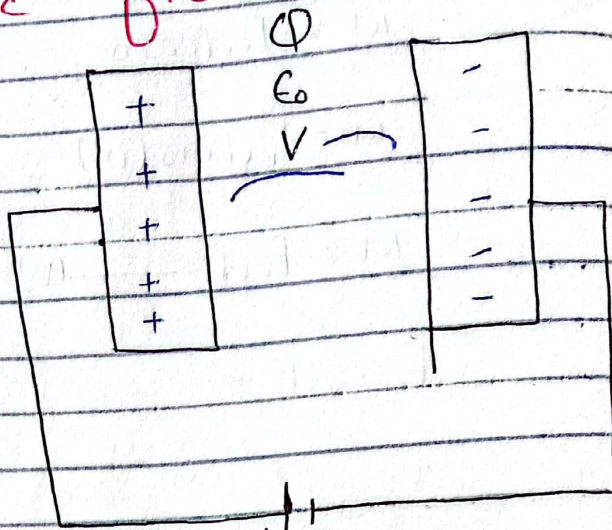
2. changing electric field produces magnetic field:

$$Q = CV \text{ --- (1)}$$

$$C_{\text{vacuum}} = \frac{A\epsilon_0}{d} \text{ --- (2)}$$

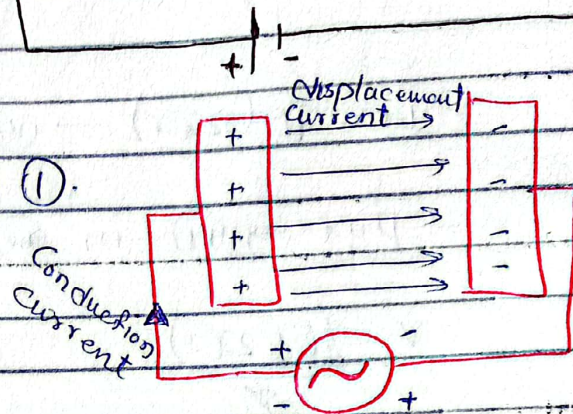
$$E = \frac{V}{d} \quad \left( E = -\frac{\Delta V}{\Delta y} \right)$$

$$V = Ed \text{ --- (3)}$$



put (2) and (3) in (1).

$$Q = \frac{A\epsilon_0}{d} (Ed)$$



$$Q = A\epsilon_0 E \text{ --- (4) charge store on capacitor}$$

In case of AC: there is current b/w plates (Electromagnetic waves are generated)

$$I = \frac{\Delta Q}{\Delta t} \text{ --- (5)}$$

$$I = \frac{\Delta}{\Delta t} (A\epsilon_0 E)$$

$$I = \epsilon_0 A \left( \frac{\Delta E}{\Delta t} \right) \text{ --- (6) } I = \frac{\epsilon_0 \Delta(\Phi)}{\Delta t}$$

$\frac{\Delta Q}{\Delta t}$  equivalent to I

The I produce magnetic field in capacitor which can be calculated from Ampere law



$$B = \frac{\mu_0 I}{2\pi r} \quad \text{--- (7)}$$

$$B = \frac{\mu_0 \epsilon_0 A}{2\pi r} \left( \frac{\Delta E}{\Delta t} \right)$$

$$B = \frac{\mu_0 \epsilon_0 A}{2\pi r} \left( \frac{\Delta E}{\Delta t} \right) \Rightarrow B = \frac{\mu_0 \epsilon_0}{2\pi r} \left( \frac{\Delta \Phi_e}{\Delta t} \right)$$

Induced magnetic field

Maxwell 2nd equation:

\* When a charge particle is moving with uniform velocity  $\rightarrow$  it is associated with constant  $E$  and  $B$  and vice versa.

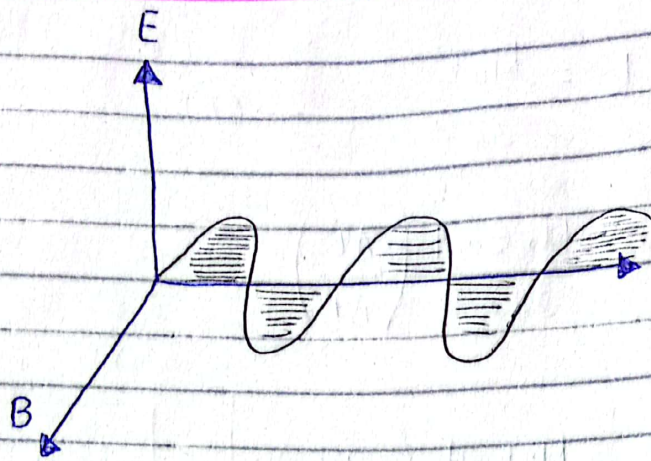
\* Electromagnetic waves are emitted when a charge particle is accelerated or decelerated...

Velocity of Electromagnetic waves:-

$$\text{As } E = \frac{A}{2\pi r} \left( \frac{\Delta B}{\Delta t} \right) \quad \text{--- (1)}$$

$$B = \frac{\mu_0 \epsilon_0 A}{2\pi r} \left( \frac{\Delta E}{\Delta t} \right) \quad \text{--- (2)}$$





Varying  $E$  produce  $B$ .

And varying  $B$  produce  $E$ .

\*  $E$ ,  $B$  and propagation of waves are perpendicular to each other.

Velocity of Electromagnetic Waves:

$$E = \frac{A}{2\pi r} \left( \frac{\Delta B}{\Delta t} \right) \quad \text{--- (1)}$$

$$B = \frac{\mu_0 \epsilon_0 A}{2\pi r} \left( \frac{\Delta E}{\Delta t} \right) \quad \text{--- (2)}$$

Divide (1) by (2):

$$\frac{E}{B} = \frac{\frac{A}{2\pi r} \left( \frac{\Delta B}{\Delta t} \right)}{\frac{\mu_0 \epsilon_0 A}{2\pi r} \left( \frac{\Delta E}{\Delta t} \right)}$$

$$= \frac{A}{2\pi r} \left( \frac{\Delta B}{\Delta t} \right) \times \frac{2\pi r}{\mu_0 \epsilon_0 A} \left( \frac{\Delta E}{\Delta E} \right)$$

$$= \frac{\cancel{A}}{2\pi r} \frac{\cancel{\Delta t}}{\cancel{\Delta t}} \left( \frac{B}{E} \right) \times \frac{2\pi r}{\mu_0 \epsilon_0 A} \frac{\cancel{\Delta t}}{\cancel{\Delta t}} \left( \frac{E}{E} \right)$$

$$\boxed{\frac{E}{B} = \frac{1}{\mu_0 \epsilon_0} \left( \frac{B}{E} \right)}$$



$$\frac{E}{B} = \frac{N}{C} \div \frac{N}{C \left(\frac{m}{s}\right)}$$

$$= \frac{N}{C} \times \frac{C}{N} \times \frac{m}{s}$$

$$= \frac{N}{C} \times \frac{C}{N} \times \frac{m}{s}$$

$$\boxed{\frac{E}{B} = \frac{m}{s}}$$

$$\therefore \frac{E}{B} = v$$

Maxwell got the Nobel prize

$$\Rightarrow \left(\frac{E}{B}\right)^2 = \frac{1}{\mu_0 \epsilon_0}$$

$$\Rightarrow v = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$

$$\text{As } \mu_0 = 4\pi \times 10^{-7} \left(\frac{N \cdot s}{A \cdot m}\right)$$

$$\epsilon_0 = 8.85 \times 10^{-12} \left(\frac{C^2}{N \cdot m^2}\right)$$

$$v = \sqrt{(4\pi \times 10^{-7})(8.85 \times 10^{-12})}$$

$$\boxed{v = 3 \times 10^8 \text{ m/s}} \approx c$$

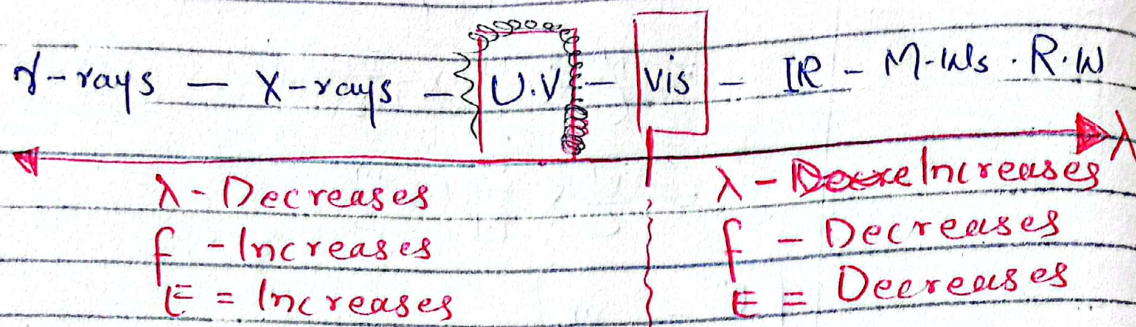
~~$$v = 8.85 \times 10$$~~

Light is also electromagnetic

in nature.



# Electromagnetic waves...



$$c = f\lambda$$

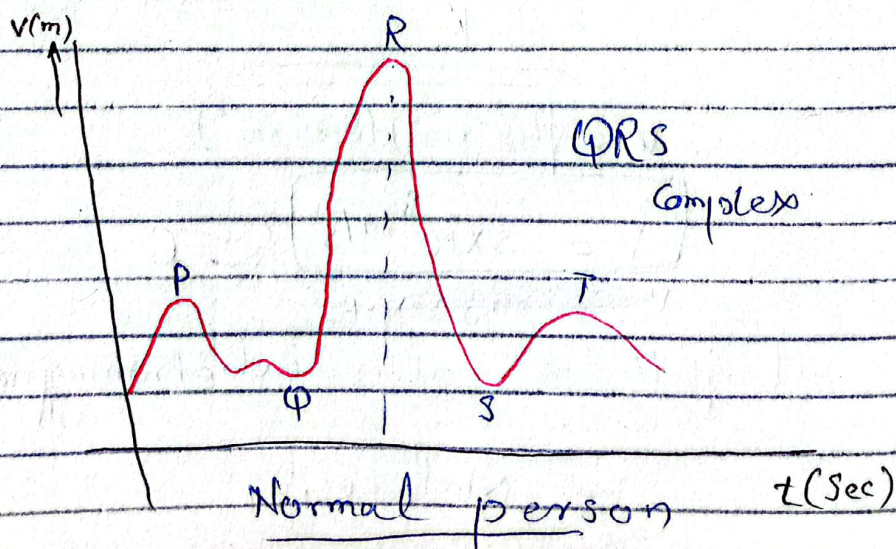
\* Velocity of all electromagnetic waves remain constant.

$\gamma$ -rays	X-rays	UV-rays	Vis	IR	M.Ws	Radio
$\lambda < 10\text{nm}$	$0.01\text{nm} - 10\text{nm}$	$1\text{nm} - 400\text{nm}$	$400\text{nm} - 700\text{nm}$	$0.7\mu\text{m} - 1\text{mm}$	$1\text{m} - 1\text{m}$	$\lambda > 1\text{m}$

25 NOV 2017

## Electrocardiogram (ECG):-

The graphical representation of the electrical activity of the heart is called ECG.





MCO #2

$$I_0 = 5\sqrt{2} \text{ A}$$

$\langle I^2 \rangle$  ?

$$\langle I^2 \rangle = \frac{0 + I_0^2}{2}$$

$$\langle I^2 \rangle = \frac{I_0^2}{2}$$

$$\langle I^2 \rangle = \frac{(5\sqrt{2})^2}{2}$$

$$\langle I^2 \rangle = (5)^2$$

$$\boxed{\langle I^2 \rangle = 25}$$

MCO #3

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{1}{LC}}$$

$$f_0 = \frac{1}{2\pi} \frac{1}{\sqrt{LC}} = f_0 \text{ will remain same}$$

MCO #7:

$$v = 20 \sin(157t)$$

$$v = v_0 \sin \omega t$$

$$v = v_0 \sin 2\pi f t$$

$$v_0 \sin 2\pi f t = 20 \sin(157t)$$

$$v_0 = 20$$

$$\sin 2\pi f t = \sin(157t)$$

$$2\pi f t = 157t$$

$$f = \frac{157}{6.28}$$

$$\boxed{f = 25 \text{ Hz}}$$

$$(2\pi f = 157)$$